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Novel color-tunable Gd₂O₂CN₂:Tb³⁺, Eu³⁺ phosphors: Characterization and

photoluminescence properties

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Abstract

In this paper, color-tunable Gd₂O₂CN₂:Tb³⁺,Eu³⁺ phosphors were obtained by co-doping Eu³⁺ and Tb³⁺

ions into Gd₂O₂CN₂ host and singly varying the Eu³⁺ doping concentration. The characteristics of the

crystal structure, photoluminescence lifetime and photoluminescence of Tb3+,Eu3+ single-doped and

 Tb^{3+} and Eu^{3+} co-doped $Gd_2O_2CN_2$, were carefully investigated by XRD, FTIR, PL decay curves and

photoluminescence (PL). The results indicated that Tb³⁺ single-doped Gd₂O₂CN₂ phosphor show a

green emission, and by increasing Eu³⁺ content, Gd₂O₂CN₂:Tb³⁺, Eu³⁺ phosphors emit green to orange

and then to red light under the excitation of 379nm.

Keywords: Photoluminescence; Gd₂O₂CN₂:Tb³⁺, Eu³⁺; color-tunable phosphors

1. Introduction

During the past few years, rare earth oxycyanamide compounds as host materials have received

much attention due to their outstanding luminescence properties when doped with rare-earth

ions[1-3]. The structures of RE₂O₂CN₂ and RE₂O₂S are closely related [4] and previous work has

shown that the luminescence properties of $RE_2O_2S:Eu^{3+}$ (RE=Gd and Y) and $RE_2O_2CN_2:Eu^{3+}$ (RE=Gd and Y) are quite similar [5, 6]. Therefore, such oxycyanamide compounds are considered to be efficient host candidates for rare-earth activators ions such as Eu^{3+} and Tb^{3+} for instance. Eu^{3+} is considered as an important activator ion with red emission corresponding to the transition of ${}^5D_0-{}^7F_J$ (J=1-6) [7]. The emission of Tb^{3+} is due to the transition between the emitting states of 5D_j and the excited states of 7F_j , and the main intense green emission is attributed to the transition of ${}^5D_4-{}^7F_5$ which is located at ca. 543nm[8].

In the previous study, we have reported the strong red emission of Eu³⁺ doped Gd₂O₂CN₂ phosphors [9]. In this work, we report a new color tunable phosphor Gd₂O₂CN₂: Tb³⁺, Eu³⁺. A series of Tb³⁺, Eu³⁺ singly-doped and Tb³⁺-Eu³⁺ co-doped phosphors were successfully prepared by classical solid state reaction at low firing temperature(750 °C). The emitting color of Gd₂O₂CN₂: Tb³⁺, Eu³⁺ phosphors can be tuned from green to orange and then to red by singly varying the doping concentration of Eu³⁺. The mechanism of energy transfer between Tb³⁺ and Eu³⁺ was investigated, and the results show that Eu³⁺/Tb³⁺ co-doped Gd₂O₂CN₂ phosphors could serve as potential phosphors for NUV LEDs.

2. Experimental

Powder samples with the general formula $Gd_{2-x}Tb_xO_2CN_2$ [x=0.03(T-1), 0.05(T-2), 0.07(T-3), 0.12(T-4), 0.15(T-5) and 0.20 (T-6)], $Gd_{1.90}Eu_{0.1}O_2CN_2$ (GOCN-4) and $Gd_{1.85-y}Tb_{0.15}Eu_yO_2CN_2$ [y=0.02(ET-1), 0.04(ET-2), 0.06(ET-3), 0.08(ET-4), 0.10(ET-5), 0.15(ET-6) were prepared by solid state reaction. High purity GdF_3 (99.99%), Eu_2O_3 (99.99%), Tb_4O_7 (99.99%), Li_2CO_3 (99.99%), and active carbon (CARBIO 12 SA—ref: C1220 G 90) as the raw materials were thoroughly mixed and fired at 600 °C for 9 h, then 750 °C for 12 h under NH₃ atmosphere. The

detailed synthesis routes can be found in literature [9].

Powder X-ray diffraction (XRD) data were recorded using a Bruker AXS D8 Advance diffractometer (Voltage 50 kV, current 40 mA, Cu-Ka). Photoluminescence (PL) and photoluminescence excitation (PLE) spectra were measured by a Fluorolog-3-P UV-vis-NIR fluorescence spectrophotometer (Jobin Yvon, longjumeau, France) with a 450 W Xenon lamp as the excitation source. The decay curves of Tb³⁺ emission was performed by FLSP920 (Edinburgh Instruments). The FTIR spectrum was measured in transmission mode using a KBr standard (Bruker, Model vector 22). The color chromaticity coordinates were obtained according to Commission Internationale de l'Eclairage (CIE) using Radiant Imaging color calculator software.

3. Results and discussion

As shown in Figure 1, the XRD patterns of the Tb³⁺ and/or Eu³⁺ activated Gd₂O₂CN₂ samples can be readily indexed as a trigonal phase and identified as Gd₂O₂CN₂ with the space group P-3m1 according to the JCPSQ database(PDF#49-1169). Considering the similar coordinated environment, electronegativity and ionic radii of Gd³⁺ (r=0.100nm, CN=7), Tb³⁺ (r=0.098nm, CN=7) and Eu³⁺(r=0.101nm, CN=7) ions, doping Tb³⁺ and Eu³⁺ does not result in any phase transformation and only has minor influence to the crystal structure.

Figure 2 shows the IR spectra of GOCN-4, ET-5 and T-5. IR spectra for ET-5 and T-5 both have the intense peaks at 2080 and 652 cm⁻¹. In our previous study we reported that the typical absorption peaks in the vicinity of 2010 and 652 cm⁻¹ in the GOCN-4 were respectively assigned to the v_2 (bending vibration) and v_3 (asymmetric stretching vibration) modes of the CN_2^{2-} ion [9]. Hence, the IR spectra also indicate that CN_2^{2-} ions contained in Eu^{3+} , Tb^{3+} single-doped and Eu^{3+} - Tb^{3+} co-doped $Gd_2O_2CN_2$ samples.

Figure 3 illustrates the excitation (monitored at 543 nm) and emission (excited by 280, 313 and 365 nm) spectra of the T-5 sample (7.5 at. % Tb³⁺). The excitation spectrum (Fig. 3a) exhibits a broad and intense band in the range from 250 to 300 nm with a peak at around 280 nm. This broad band is attributed to $4f^8$ - $4f^75d^1$ transitions of Tb³⁺ ions. The other excitation bands at longer wavelengths, are located at 307 nm ($^5H_5 \rightarrow ^7F_6$), 313 nm ($^5H_5 \rightarrow ^7F_5$) and 350-380nm (transitions from 7F_4 , 7F_3 to 5H_7 , 5D_0 , 5D_1). The emission spectra of T-5 (Fig. 3b) at different excitation wavelengths are very similar both in shape and relative intensities. The strongest peak split into two at 543 and 550 nm corresponds to the $^5D_4 \rightarrow ^7F_5$ transition, while the peaks at 487 and 495nm, 587nm, and 622nm respectively originate from the $^5D_4 \rightarrow ^7F_6$, $^5D_4 \rightarrow ^7F_4$ and $^5D_4 \rightarrow ^7F_3$ transitions of Tb³⁺ ions.

The excitation (monitored at 543nm) and emission (monitored at 280nm) spectra of $Gd_{2-x}Tb_xO_2CN_2$ with varying Tb^{3+} concentrations (x=0.03, 0.05, 0.07, 0.12, 0.15 and 0.20) are shown in Fig. 4. With the increase of doped Tb^{3+} ions concentration, the excitation and the emission intensity increases gradually ranging from 1.5 to 7.5 at. % and decreases from 7.5 to 10 at. %, which is in accordance with Eu^{3+} doped $Gd_2O_2CN_2$ in previous work [9]. Considering the mechanism of energy transfer in phosphors, the concentration quenching can be explained in more details by the critical distance (R_c) between Tb^{3+} ions which can be calculated by Eq. (1) [10]:

$$R_c = 2 \times (3V / 4\pi X_c N)^{1/3}$$
 (1)

Where V (101.9 Å³) is the volume of the unit cell, X_c (0.075) is the critical concentration of Tb^{3+} ions and N (2) is the number of lattice sites in the unit cells that can be occupied by Tb^{3+} ions. Therefore, R_c between Tb^{3+} ions is calculated to be 10.907 Å.

PL and PLE spectra of singly-doped Eu³⁺ (GOCN-4, 5 at. %) or Tb³⁺ (T-5, 7.5 at. %) and

Eu³⁺/Tb³⁺ (ET-1, 1at. %/ 7.5 at. %) co-doped $Gd_2O_2CN_2$ phosphors are presented in Fig. 5. The excitation spectrum of GOCN-4 exhibits a broad and intense band in the range from 250 to 350 nm with a peak at around 300 nm, which is attributed to the ligand-to-metal charge transfer between O^2 and Eu^{3+} . The weak excitation bands at longer wavelength corresponding to the 4f-4f transitions of Eu^{3+} are located at 379nm (${}^7F_0 \rightarrow {}^5G_2$), 395nm (${}^7F_0 \rightarrow {}^5L_6$), 467nm (${}^7F_0 \rightarrow {}^5D_2$). Upon excitation at 300nm, the emission spectrum shows two strong peaks at 614 and 626 nm which originate from the ${}^5D_0 \rightarrow {}^7F_2$ transition of Eu^{3+} . Fig. 5 (b) shows the excitation and emission spectra of T-5, an intensive broad excitation band with the maximum at 280nm and other peaks at 313 and 379nm are observed. Upon the excitation at 280nm, the emission spectrum shows a strong peak at 543nm which is attributed to the transition ${}^5D_4 - {}^7F_5$ of Tb³⁺. Fig. 5 (c) shows the excitation spectra of ET-1 monitored at 626 and 543nm, the excitation band at around 379nm can be observed in both excitation spectra. The emission spectrum of ET-1 shows typical peaks at 543nm that originated from transition ${}^5D_4 - {}^7F_5$ of Tb³⁺ and at 614 and 626nm from transition ${}^5D_0 \rightarrow {}^7F_2$ of Eu³⁺.

The emission spectra of $Gd_{1.85\text{-y}}Tb_{0.15}Eu_yO_2CN_2$ ($0 \le y \le 0.15$) are illustrated in Fig. 6. All samples exhibit two prominent peaks peaking at 543 and 626nm under 379nm excitation. By increasing the concentration of Eu^{3+} , the emission intensities of Tb^{3+} at 543nm decrease remarkably while the emission intensity of Eu^{3+} at 626nm initially increases and then reaches a maximum at y=0.10, then decreases due to the concentration quenching. Therefore, we can speculate about the existence of energy transfer from Tb^{3+} to Eu^{3+} cations, such an energy transfer has also been observed in $Y_2O_3[11]$, $Ca_8MgLu(PO_4)_7$ [12]and $SrMg_2La_2W_2O_{12}$ host materials[13].

To further certify the energy transfer from Tb^{3+} to Eu^{3+} ions in $Gd_2O_2CN_2$ host matrix, the PL decay curves were measured (excited at 379nm and monitored at 543nm) and the lifetimes of

different samples were calculated. Fig. 7 shows the decay curves of Tb³⁺ ions which can be well fitted to a double-exponential function as the following equation [14]:

$$I = I_0 + A_1 \exp(-t/\tau_1) + A_2 \exp(-t/\tau_2)$$
 (1)

Where I is the luminescent intensity at the time of t and I_0 is the luminescent intensity at the time of 0; A_1 and A_2 are fitting parameters; τ_1 and τ_2 are rapid and slow lifetimes for exponential components, respectively. Based on these parameters, the average lifetime of Tb^{3+} ions with different Eu^{3+} concentration can be calculated by the following equation:

$$\tau = (A_1 \tau_1^2 + A_2 \tau_2^2) / (A_1 \tau_1 + A_2 \tau_2) \tag{2}$$

The effect of Eu³⁺ content on the calculated Tb³⁺ ions lifetimes was shown in the Fig. 7 inset, the decay lifetime of Tb³⁺ ions decrease with increasing Eu³⁺ concentration, which strongly supported the energy transfer from Tb³⁺ ions to Eu³⁺ ions.

Table 1 summarizes the CIE chromaticity coordinates of $Gd_{1.85\text{-y}}Tb_{0.15}Eu_yO_2CN_2$ ($0 \le y \le 0.20$) phosphors under the excitation at 379nm, Figure 8 also gives the CIE chromaticity coordinates, and it is interesting to notice that with the increasing of Eu^{3+} ions concentration, the CIE chromaticity coordinates shift from (0.3134, 0.5454) to (0.5682, 0.3322), the emitting color turned from green to red accordingly. The inset of Fig. 8 also shows the digital photos of $Gd_{1.85}Tb_{0.15}O_2CN_2$ (a), $Gd_{1.83}Tb_{0.15}Eu_{0.02}O_2CN_2$ (b) and $Gd_{1.70}Tb_{0.15}Eu_{0.15}O_2CN_2$ (g) phosphors under excitation at 379nm light. With the development of chip technology, high-performance InGaN-based 380 nm UV LEDs are fabricated [15] and commercially available NUV InGdN LED chip from 375 to 380nm is more and more common. Therefore, Eu^{3+} , Tb^{3+} co-doped $Gd_2O_2CN_2$ phosphors may have potential applications for NUV LEDs.

4. Conclusion

In this paper, Eu³⁺, Tb³⁺ singly doped and Eu³⁺-Tb³⁺ co-doped Gd₂O₂CN₂ phosphors were successfully prepared by classical solid-state reaction. The Tb³⁺ doped Gd₂O₂CN₂ phosphors exhibit a characteristic green emission with the strong peak at 543nm. The optimized Tb³⁺ concentration of Gd₂O₂CN₂:Tb³⁺ is 7.5 at. %. When Eu³⁺ and Tb³⁺ were co-doped into Gd₂O₂CN₂, an efficient energy transfer from Tb³⁺ to Eu³⁺ occurred and thus by only increasing the doping concentration of Eu³⁺, it becomes possible to tune the emission color from green to orange and then to red under the excitation at 379nm.

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FIG. 1. XRD patterns of $Gd_{1.9}Eu_{0.1}O_2CN_2$, $Gd_{1.75}Tb_{0.15}Eu_{0.1}O_2CN_2$ and $Gd_{1.85}Tb_{0.15}O_2CN_2$ (the standard data of $Gd_2O_2CN_2$ (PDF#49-1169) is shown as reference)

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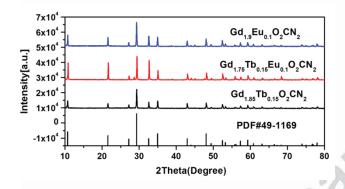


FIG. 2. FTIR spectra of Gd_{1.9}Eu_{0.1}O₂CN₂, Gd_{1.75}Tb_{0.15}Eu_{0.1}O₂CN₂ and Gd_{1.85}Tb_{0.15}O₂CN₂ samples

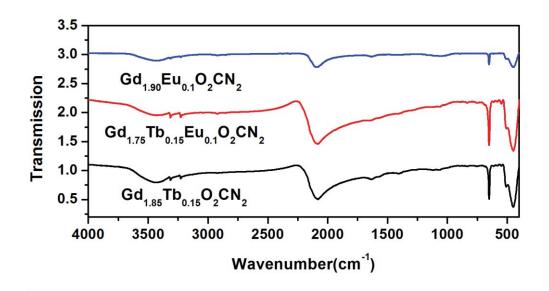


FIG. 3. Excitation (a) and Emission (b) spectra of the $Gd_{1.85}Tb_{0.15}O_2CN_2$ sample. The right inset is the photograph image of the Tb^{3+} -doped sample being excited by the 280nm lights.

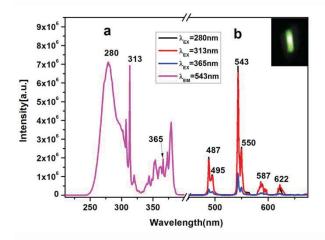
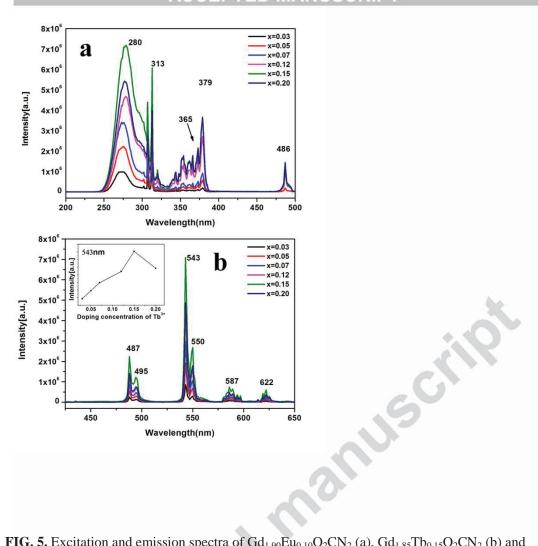


FIG. 4. Excitation (a) and emission (b) spectra of $Gd_{2-x}Tb_xO_2CN_2$ (x=0.03, 0.05, 0.07, 0.12, 0.15, 0.200) samples. The inset is the dependence of its PL intensity on the Tb^{3+} content in the $Gd_2O_2CN_2$ matrix.



 $\label{eq:FIG.5.} \textbf{FIG. 5.} \ \text{Excitation and emission spectra of} \ Gd_{1.90}Eu_{0.10}O_{2}CN_{2} \ (a), \ Gd_{1.85}Tb_{0.15}O_{2}CN_{2} \ (b) \ \text{and}$ $Gd_{1.83}Eu_{0.02}Tb_{0.15}O_{2}CN_{2} \ (c)$

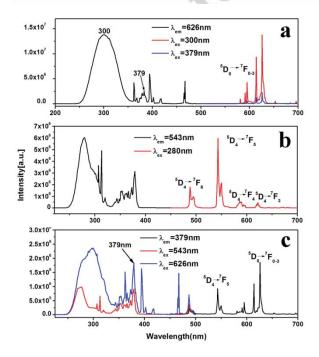


FIG. 6. Emission spectra of $Gd_{1.85-y}Tb_{0.15}Eu_yO_2CN_2$ (y=0, 0.02, 0.04, 0.06, 0.08, 0.10, 0.15) samples under the excitation wavelength of 379nm

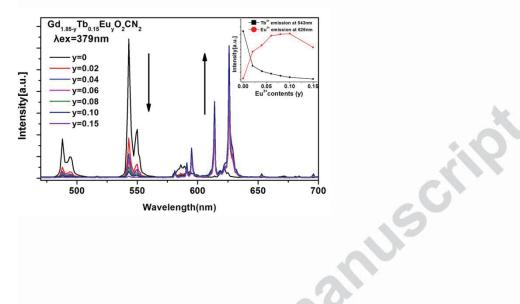


FIG. 7. Representative decay curves for the luminescence of Tb^{3+} in $Gd_{1.85}Tb_{0.15}O_2CN_2$, $Gd_{1.83}Tb_{0.15}Eu_{0.02}O_2CN_2$ and $Gd_{1.81}Tb_{0.15}Eu_{0.04}O_2CN_2$. The inset shows the lifetime of Tb^{3+} as a function of Eu^{3+} concentration in $Gd_2O_2CN_2$ host matrix (excited at 379 nm and monitored at 543 nm).

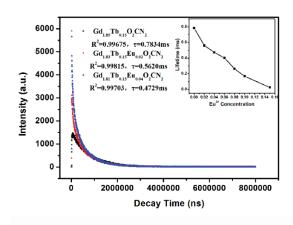


FIG. 8. CIE chromaticity coordinate digram of $Gd_{1.85-y}Tb_{0.15}Eu_yO_2CN_2$ (y=0, 0.02, 0.04, 0.06, 0.08, 0.10, 0.15) samples under the excitation at 379nm (the inset shows the digital photos of the $Gd_{1.85}Tb_{0.15}O_2CN_2$ (a), $Gd_{1.83}Tb_{0.15}Eu_{0.02}O_2CN_2$ (b) and $Gd_{1.70}Tb_{0.15}Eu_{0.15}O_2CN_2$ (g) phosphors under the excitation of 379nm light

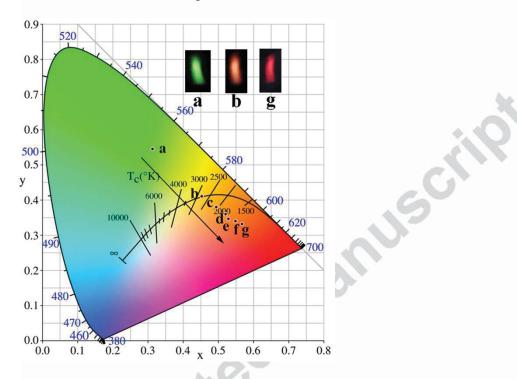


Table 1 CIE chromaticity coordinates for $Gd_{1.85-y}Tb_{0.15}Eu_yO_2CN_2$ (y=0, 0.02, 0.04, 0.06, 0.08, 0.10, 0.15) samples

Sample no.	Sample	CIE coordinates (x,y)
	composition(y)	
a (T-5)	y=0	(0.3134, 0.5454)
b (ET-1)	y=0.02	(0.4534, 0.4112)
c (ET-2)	y=0.04	(0.4953, 0.3794)
d (ET-3)	y=0.06	(0.5216, 0.3596)
e (ET-4)	y=0.08	(0.5289, 0.3469)
f (ET-5)	y=0.10	(0.5493, 0.3405)

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g (ET-6) y=0.15 (0.5682, 0.3322)

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