Copper Hyper-Stoichiometry: The Key for the Optimization of Thermoelectric Properties in Stannoidite Cu8+xFe3–xSn2S12

Ventrapati Pavan Kumar, Tristan Barbier, Vincent Caignaert, Bernard Raveau, Ramzy Daou, Bernard Malaman, Gérard Le Caër, Pierrick Lemoine, Emmanuel Guilmeau

To cite this version:

Ventrapati Pavan Kumar, Tristan Barbier, Vincent Caignaert, Bernard Raveau, Ramzy Daou, et al.. Copper Hyper-Stoichiometry: The Key for the Optimization of Thermoelectric Properties in Stannoidite Cu8+xFe3–xSn2S12. Journal of Physical Chemistry C, American Chemical Society, 2017, 121 (30), pp.16454-16461. 10.1021/acs.jpcc.7b02068. hal-01580457

HAL Id: hal-01580457
https://hal-univ-rennes1.archives-ouvertes.fr/hal-01580457
Submitted on 14 Sep 2017

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L’archive ouverte pluridisciplinaire HAL, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d’enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.
Copper Hyper-stoichiometry, the Key for the
Optimization of Thermoelectric Properties in
Stannoidite Cu$_{8+x}$Fe$_{3-x}$Sn$_2$S$_{12}$

Ventrapati Pavan Kumar,† Tristan Barbier,† Vincent Caignaert,† Bernard Raveau,† Ramzy Daou,† Bernard Malaman,‡ Gérard Le Caër,# Pierric Lemoine,§ and Emmanuel Guilmeau*,†

† Laboratoire CRISMAT, UMR 6508 CNRS/ENSICAEN, 6 bd du Marechal Juin, 14050 Caen Cedex 4, France

‡ Institut Jean Lamour, UMR 7198, CNRS, Université de Lorraine, Faculté des Sciences et Technologie, B.P. 70239, 54506 Vandœuvre-lès-Nancy Cedex, France

# Institut de Physique de Rennes, UMR UR1-CNRS 6251, Université de Rennes I, Campus de Beaulieu, Bâtiment 11A, F-35042 Rennes Cedex, France

§ Institut des Sciences Chimiques de Rennes (ISCR) - UMR CNRS 6226, Université de Rennes I, Campus de Beaulieu, Bâtiment 10A, 35042 Rennes Cedex, France

KEYWORDS. thermoelectric, sulfide, stannoidite, mechanical alloying, SPS
ABSTRACT

A univalent copper hyper-stoichiometric stannoidite Cu$_{8+y}$Fe$_{3-x}$Sn$_2$S$_{12}$ with $0 \leq x \leq 0.5$ has been synthesized using mechanical alloying followed by spark plasma sintering. The X-ray diffraction analysis combined with $^{57}$Fe and $^{119}$Sn Mössbauer investigations has allowed the charge distribution of the cationic species on the various sites to be established and suggests the possibility of a small tin deficiency. The transport properties show a remarkable crossover from a semiconducting to a metal-like behaviour as the copper content increases from $x = 0$ to $x = 0.5$, whereas correlatively the Seebeck coefficient decreases moderately, with $S$ values ranging from 310 to 100 $\mu$V/K. The thermal conductivity decreases as the temperature increases showing low values at high temperature, far below those reported in related stannite materials. The investigation of the thermoelectric properties shows that the $ZT$ figure of merit is dramatically enhanced by the copper hyper-stoichiometry by a factor of 5 going from 0.07 for $x = 0$ to 0.35 for $x = 0.5$ at 630 K. This thermoelectric behaviour is interpreted on the basis of a model involving the Cu-S framework as the conducting electronic network where the Fe$^{2+}$/Fe$^{3+}$ species play the role of hole reservoir.

1. INTRODUCTION

The demand in energy consumption has been escalating this last decade, leading to renewed interest on thermoelectric (TE) technology.$^{1}$ Beyond the promising results obtained for telluride based materials which exhibit high performances,$^{2-4}$ the need to conciliate efficiency with environmental and cost constraints has triggered research recently toward copper-based sulfides which have, for most of them, the advantage to contain eco-friendly and abundant elements. The figure of merit $ZT$ values ($ZT = S^2T/\rho\kappa$, where $S$ is the Seebeck coefficient, $T$ is the absolute
temperature, $\rho$ is the electrical resistivity and $\kappa$ is the thermal conductivity) observed for the simple phases $\text{Cu}_{2.5}\text{S}$, ranging from 0.5 to 1.7 $^{5-7}$ are very attractive. However, the electromigration of copper that appears in the Cu-S system weakens the stability and durability of these TE materials. The introduction of other metallic (M) elements besides copper has allowed this problem to be mostly overcome, opening the route to the exploration of complex copper based sulfides. Actually, from the viewpoint of thermoelectricity, two classes of copper based sulfides can be distinguished exhibiting an n-type and p-type conductivity, respectively. The n-type class is obtained for lower copper content materials, i.e. Cu/M ratio $\leq 1$, as shown for chalcopyrite CuFeS$_2$-type sulfides such as CuFe$_{1-x}$In$_x$S$_2$ $^8$ and Cu$_{1-x}$Zn$_x$FeS$_2$ $^9$ and for the cubic isocubanite CuFe$_2$S$_3$ $^{10}$, suggesting that the Fe 3$d$ states play a major role in the formation of the electronic band structure of these n-type thermoelectrics. The p-type class of copper based sulfides covers a broad range of compositions, from Cu/M ratio equal or close to 1 as exemplified by the stannites Cu$_2$ZnXS$_4$ (X=Sn, Ge)$^{11,12}$ and copper-rich sulfides, with Cu/M ratios ranging from 2 to 5 as shown by Cu$_2$SnS$_3$, $^{13}$ the derivatives of the tetrahedrite Cu$_{12}$Sb$_4$S$_{13}$, $^{14-16}$ of the colusite Cu$_{26}$V$_2$Sn$_6$S$_{32}$, $^{17-19}$ and of the bornite Cu$_3$FeS$_4$, $^{20-22}$

From these studies, the p-type copper rich sulfides appear as most promising for thermoelectric applications. However, the improvement of the thermoelectric performances of these materials remains a challenge, due to the interdependent and contrary effects of their electrical and thermal transport parameters $S$, $\rho$ and $\kappa$. The nature of the chemical bonds, especially Cu-S bonds and of the distribution of charges in these complex structures is still a matter of debate, which is of capital importance for the optimization of their TE properties. In this respect, the stannoidite Cu$_6$(Fe,Zn)$_3$Sn$_2$S$_{12}$ mineral appears to be an attractive material in relation with (i) its orthorhombic structure $^{23}$ (Figure 1) closely related to that of stannite, (ii) the possibility to
prepare the synthetic isostructural Cu$_8$Fe$_3$Sn$_2$S$_{12}$ sulfide, and (iii) the distribution of the cationic charges according to the formula (Cu$^+$)$_8$(Fe$^{2+}$)$_2$(Fe$^{3+}$)$_2$(Sn$^{4+}$)$_2$(S$^2$)$_{12}$ determined by Mössbauer spectroscopy. Curiously, the thermoelectric properties of this sulfide have not been investigated to date, in spite of its potential to be used as a well characterized model material for understanding the TE phenomena in these materials. We report herein on the synthesis by mechanical alloying followed by spark plasma sintering (SPS) and on the TE properties of the copper hyper-stoichiometric stannoidite Cu$_{8+x}$Fe$_{3-x}$Sn$_2$S$_{12}$ ($x \leq 0.5$) series. A drastic change in the TE properties is observed with the copper content, characterized by a crossover from a semiconducting poor TE ($ZT_{630 K} = 0.07$) state for the stoichiometric phase ($x = 0$) to a metallic-like attractive TE ($ZT_{630 K} = 0.35$) state for the Cu-hyper-stoichiometric sulfide ($x = 0.5$). The modification of these performances is explained in the frame of the iono-covalent model of the chemical bonds.

![Figure 1. View of the crystal structure of stannoidite Cu$_8$Fe$_3$Sn$_2$S$_{12}$.](image)

### 2. EXPERIMENTAL SECTION
Polycrystalline samples of Cu$_{8+x}$Fe$_{30-x}$Sn$_2$S$_{12}$ ($0 \leq x \leq 0.5$) were synthesized by mechanical alloying$^{26}$ followed by Spark Plasma Sintering. All sample preparation and handling of powders were performed in Argon filled glove box with oxygen content of < 1 ppm. Stoichiometric amounts of Cu (99.9 %, Alfa Aesar), Fe (99.9 %, Alfa Aesar), Sn (99.9 %, Alfa Aesar) and S (99.99 %, Alfa Aesar) were loaded in a 25 ml tungsten carbide jar under argon atmosphere. The powders were then milled in a high-energy planetary ball mill (Fritsch Pulverisette 7 Premium line) at a speed of 600 rpm for 12 hours. The resulting powders were then ground and sieved down to 150 µm. Powders were then placed in tungsten carbide dies of 10 mm diameter and densified by Spark Plasma Sintering (SPS – FCT HPD 25) at 873 K for 15 min under a pressure of 150 MPa (heating and cooling rate of 50 K/min and 20 K/min, respectively). This produced 10 mm diameter pellets, ca. 7 mm thick, with geometrical densities greater than 98 %. It is worth pointing out that these samples are air sensitive and contain small traces of SnO$_2$.

The crystalline phases were identified at room temperature by powder X-ray diffraction (PXRD) using a X’Pert Pro PANalytical diffractometer using Co Kα radiation ($\lambda = 1.78901$ Å). Data were collected over the angular range $5 \leq 2\theta/° \leq 100$ with a step size of 0.0131° and a step time of 250 s, using a rotating sample holder in order to increase accuracy of the measurements. Rietveld refinements from data collected on the sintered samples have been performed using FullProf and WinPlotr software packages.$^{27,28}$

Seebeck coefficient and electrical resistivity were measured under helium atmosphere using steady state technique and four probe method, respectively, (ZEM-3, ULVAC-RIKO, Japan) over the temperature range of 300 K to 650 K on a 9×3×3 mm$^3$ sample. The thermal diffusivity ($D$) of a square sample (6×6×1 mm$^3$) was measured from 300 K to 650 K in an inert atmosphere using a Netzsch LFA457 apparatus. Heat capacity ($C_p$) was calculated using Dulong-Petit
approximation. Thermal conductivity ($\kappa$) was calculated from the product of the sample density ($d$), thermal diffusivity ($D$) and heat capacity ($C_p$). The combined uncertainty in the determination of the $ZT$ values is estimated to be 17\%.\textsuperscript{29}

Room temperature Hall effect measurements were carried out using Physical Properties Measurement System (PPMS; Quantum Design) under an applied magnetic field up to 9T. However, it is difficult to extract reliable carrier concentrations from the Hall effect data since the samples are magnetic and the contribution of the anomalous Hall effect appears to be significant. Attempts to calculate the carrier concentration using the approximation of single parabolic band conduction model, using the formula $p = 1/R_H e$, where $e$ is the electronic charge; gives an unrealistically high value of $p = 7.8 \times 10^{19}$ cm$^{-3}$, suggesting a very strong anomalous contribution. Values for $x = 0.3$ and $x = 0.5$ appear to be more reasonable but could be overestimated ($p = 1.2 \times 10^{22}$ cm$^{-3}$ and $1.1 \times 10^{22}$ cm$^{-3}$). Due to the linearity of the Hall signal with magnetic field, it is nevertheless difficult to account for the anomalous contribution. Another possibility is that two types of carrier are present, which could also cause the carrier concentration to be overestimated. Low temperature or very high magnetic field studies are required to confirm which effect is relevant.

$^{57}$Fe and $^{119}$Sn Mössbauer spectra were measured at $T = 300$ K in transmission geometry with a spectrometer operated in the conventional constant-acceleration mode. Some $^{57}$Fe spectra were recorded at 80 K thanks to a JANIS (research company inc.) liquid helium cryostat. Polycrystalline absorbers, with natural abundance of $^{57}$Fe or $^{119}$Sn isotope and thickness of ~15 mg cm$^{-2}$, were used. Sources were kept at room temperature ($RT$) to collect either $^{57}$Fe or $^{119}$Sn Mössbauer spectra. For $^{57}$Fe spectra, the source was $^{57}$Co in Rh matrix with a nominal strength of 25 mCi. For $^{119}$Sn spectra, the source was Ba$^{119m}$SnO$_3$ with a nominal strength of 10 mCi. A
palladium foil of 0.5 mm thickness was used as a critical absorber for tin X-rays. Velocity calibration was performed against a 12 µm-thick α-Fe foil at RT. $^{57}$Fe and $^{119}$Sn isomer shifts (δ) are referred respectively to α-Fe and to BaSnO$_3$ at RT. Mössbauer spectra were fitted with a least-squares method program assuming Lorentzian peaks.

3. RESULTS AND DISCUSSION

3.1. Structural Analysis

High-energy ball-milling of elemental powder mixture with stoichiometry ranging from Cu$_8$Fe$_3$Sn$_2$S$_{12}$ to Cu$_{8.5}$Fe$_{2.5}$Sn$_2$S$_{12}$ produces fine black powders. Typical X-ray powder diffraction pattern of these samples is presented in Figure S1. Then, SPS performed at 873 K on the seven Cu$_{8+x}$Fe$_{3-x}$Sn$_2$S$_{12}$ samples, not only leads to compact pellets, but also allows to obtain highly pure and well-crystallized stannoidite samples. This synthesis process was previously proved to be efficient to prepare large quantity of high purity samples of other ternary and quaternary sulfides.$^{18,22,30-32}$ The PXRD pattern of $x = 0$ (Figure 2) and $x = 0.3$ samples (Figure S2) are characteristic of the stannoidite structure and could be indexed in an orthorhombic unit-cell with the space group $I222$. Our unit-cell parameters for $x = 0$ sample ($a = 10.758(1)$ Å; $b = 5.3971(2)$ Å; $c = 16.135(2)$ Å, Table S1) are also comparable with those previously reported for natural stannoidite minerals, and present only small deviations due to slightly different chemical compositions. As shown by previous studies,$^{23,25}$ the crystal structure of stannoidite is closely related to that of stannite. A blow up of the low intensity region from 17° to 32°, (insets Figure 2 and S2), shows the superstructure diffraction peaks of the stannoidite with respect to the stannite phase ($I42m$). These superstructure reflections, indexed with $h,k,l = 3n+1$ and $h,k,l = 3n+2$, are broadened with respect to the main reflections, indexed with $h,k,l = 3n$. This broadening of the
superstructure reflections may indicate presence of atomic disorder or crystallographic defects. For the Rietveld refinements from PXRD data, the occupancy factors of the cationic sites were kept unchanged with respect to the mineral, since copper and iron cannot be distinguished one from the other from XRPD data due to their very close atomic numbers. From these refinements, the overall B factor converged to a reasonable value ($B = 0.78(8)$ Å$^2$ for $x = 0$). This supports that the existing cationic disordering is limited. The refined atomic coordinates, cell parameters and reliability factors for $x = 0$ and $x = 0.3$ are listed in Table S1 and S2. It is worth pointing out that the cell parameters decrease as $x$ increases, i.e. as Fe$^{2+}$ is replaced by the couple Fe$^{3+}$/Cu$^+$, in agreement with the size of the metallic cations.

These first results attest that the crystallographic structure of these synthetic sulfides is equivalent to that previously described by Kudoh and Takeuchi$^{23}$ for the mineral stannoidite and consists of edge-sharing CuS$_4$, SnS$_4$ and FeS$_4$ ordered tetrahedra, where metallic atoms are distributed on seven different crystallographic sites. Thus the structure of stoichiometric Cu$_8$Fe$_3$Sn$_2$S$_{12}$ (Figure 1) can be described as the stacking along the $a$ axis of pure tetrahedral univalent copper layers alternating with mixed tetrahedral layers containing copper, tin and iron.
Figure 2. Rietveld refinement of $\text{Cu}_8\text{Fe}_3\text{Sn}_2\text{S}_{12}$: as usual, red dots, black and blue curves represent the observed, calculated and difference plots, respectively. The green vertical lines represent the position of the Bragg reflections. Top lines are reflections of the stannoidite: short lines are $h,k,l=3n+1$ and $h,k,l=3n+2$ reflections while large lines are $h,k,l=3n$ reflections. Bottom lines are reflections of the SnO$_2$ impurity. The inset shows the broadening of the $h,k,l$ reflections with $l=3n+1$ and $l=3n+2$ (white arrows) and the main reflection of the SnO$_2$ impurity (< 1% wt., black arrow).

3.2. Mössbauer Spectroscopy Characterizations

We performed a Mössbauer study of copper hyper stoichiometric sulfides $\text{Cu}_{8+x}\text{Fe}_{30}x\text{Sn}_2\text{S}_{12}$ for $x = 0, 0.3$ and $0.5$ to follow the evolution of charge distributions with $x$. The $^{119}\text{Sn}$ RT Mössbauer spectra of all three samples evidence only a narrow quadrupolar doublet, with a full width at half maximum (FWHM) of $\sim 0.9 \text{ mm.s}^{-1}$, an isomer shift $\text{IS} = 1.42 \pm 0.02 \text{ mm.s}^{-1}$ and a quadrupole splitting (QS) of $0.42 \pm 0.02 \text{ mm.s}^{-1}$. This isomer shift value is characteristic of tin atoms in a $+IV$ oxidation state, in fair agreement with the one, $1.48 \pm 0.05 \text{ mm.s}^{-1}$ reported for $\text{Cu}_8\text{Fe}_3\text{Sn}_2\text{S}_{12}$.\textsuperscript{25} Yamanaka and Kato emphasize that $^{119}\text{Sn}$ isomer shifts in stannite $\text{Cu}_2(\text{Fe,Zn})\text{SnS}_4$ (Zn/Fe=0.3), stannoidite $\text{Cu}_8(\text{Fe,Zn})_3\text{Sn}_2\text{S}_{12}$ (Zn/Fe=0.07), and mawsonite $\text{Cu}_6\text{Fe}_2\text{SnS}_8$, which ranges from $1.45 \pm 0.03 \text{ mm.s}^{-1}$ to $1.48 \pm 0.03 \text{ mm.s}^{-1}$, support the assumption of a strongly covalent SnS$_4$-tetrahedron in these minerals. Similarly, the $^{119}\text{Sn}$ isomer shift in the sulfide $\text{Cu}_2\text{FeSnS}_4 ((\text{Cu}^+)_2(\text{Fe}^{2+})(\text{Sn}^{4+})(\text{S}^2-)_4)$ is $\text{IS} = 1.48 \pm 0.03 \text{ mm.s}^{-1}$.\textsuperscript{33} We conclude finally that the aforementioned isomer shifts are consistent with typical values, $\sim 1.3 \text{ mm.s}^{-1}$, obtained for tetrahedral Sn(IV)S$_4$ and discussed theoretically by Lippens.\textsuperscript{34} A
representative $^{119}$Sn Mössbauer spectrum is shown in Figure 3, where a small amount of SnO$_2$ ($\sim$ 2% of Sn atoms) is observed as explained in the experimental section.

![Figure 3. RT $^{119}$Sn Mössbauer spectrum of Cu$_8$Fe$_3$Sn$_2$S$_{12}$](image)

$^{57}$Fe Mössbauer spectra of Cu$_{8+x}$Fe$_{3-x}$Sn$_2$S$_{12}$ are shown in Figure 4a and 4b at 300K for $x = 0$, 0.3 and 0.5, and at 80 K for $x = 0$ and 0.3, respectively. Typical FWHM’s range between $\sim 0.25$ mm.s$^{-1}$ and 0.35 mm.s$^{-1}$. Lamb-Mössbauer factors are needed to convert relative spectral areas of the various components of $^{57}$Fe Mössbauer spectra into iron abundances. We assume that these factors have here similar values for Fe$^{2+}$ and Fe$^{3+}$ (see ref.$^{25}$) so that relative abundances coincide with relative areas. Hyperfine parameters and relative areas obtained from spectra fittings are given in Table 1 for $T = 80$ K and 300 K. The moderate temperature variation of the relative areas between 300K and 80K supports the above assumption.

An outer doublet with a large quadrupole splitting, QS $\sim$ 2.9 mm.s$^{-1}$ and an isomer shift IS $\sim$ 0.6 mm.s$^{-1}$ at $RT$ is observed for $x < 0.5$ (Table 1). The latter is then attributed to Fe$^{2+}$. Its
quadrupole splitting agrees with those reported by Yamanaka and Kato\textsuperscript{25} for Fe\textsuperscript{2+} in stannoidite Cu\textsubscript{8}(Fe,Zn)\textsubscript{3}Sn\textsubscript{2}S\textsubscript{12} (Zn/Fe = 0.3) and in Cu\textsubscript{8}Fe\textsubscript{3}Sn\textsubscript{2}S\textsubscript{12}, both being 2.86 ± 0.08 mm.s\textsuperscript{-1}. In addition, it is quite close to QS = 2.87 ± 0.03 mm.s\textsuperscript{-1} measured for Fe\textsuperscript{2+} in Cu\textsubscript{2}FeSnS\textsubscript{4} ((Cu\textsuperscript{+})(Fe\textsuperscript{2+})(Sn\textsuperscript{4+})(S\textsuperscript{2-})\textsubscript{4}) by Eibschütz et al.\textsuperscript{33}

![Figure 4. 57Fe Mössbauer spectra of Cu\textsubscript{8-x}Fe\textsubscript{x}Sn\textsubscript{2}S\textsubscript{12} with x increasing from left to right (a) top row, at 300 K for x = 0, 0.3 and 0.5 and b) bottom row, at 80 K for x = 0 and 0.3](image)

When copper excess is substituted for iron in Cu\textsubscript{8}Fe\textsubscript{3}Sn\textsubscript{2}S\textsubscript{12} to yield Cu\textsubscript{8-x}Fe\textsubscript{x}Sn\textsubscript{2}S\textsubscript{12}, the relative values of the redox potential of the Cu\textsuperscript{2+}/Cu\textsuperscript{+} and Fe\textsuperscript{3+}/Fe\textsuperscript{2+} couples favour the oxidation of Fe\textsuperscript{2+} by Cu\textsuperscript{2+} as the equilibrium Cu\textsuperscript{2+} + Fe\textsuperscript{2+} ⇌ Cu\textsuperscript{+} + Fe\textsuperscript{3+} (1) is strongly displaced toward the right. \textsuperscript{57}Fe Mossbauer spectra of three samples with x = 0, 0.3 and 0.5 (Figure 4a) confirm that
the Fe$^{2+}$ content decreases at the expense of the Fe$^{3+}$ content (Table 1) as expected when copper (Cu$^+$) substitutes for iron. Thus, from the viewpoint of major charges, the formula of a copper hyper stoichiometric phase can be formally written as $(\text{Cu}^+)_{8+x}(\text{Fe}^{2+})_{1-2x}(\text{Fe}^{3+})_{2x}(\text{Sn}^{4+})_2(S^2)_12$. As a consequence, a Cu substitution limit is reached in $(\text{Cu}^+)_{8.5}(\text{Fe}^{3+})_{2.5}(\text{Sn}^{4+})_2(S^2)_12$ with $x = 0.50$, a value for which the Fe$^{2+}$ species is predicted to disappear in agreement with experimental results (Figure 4a, $T = 300$K).

A first notable result is that the relative area of the Fe$^{2+}$ component, called here $A^{2+}(x)$, is clearly smaller than the one, $(1-2x)/(3-x)$, expected from the sulfide formula $(\text{Cu}^+)_{8+x}(\text{Fe}^{2+})_{1-2x}(\text{Fe}^{3+})_{2x}(\text{Sn}^{4+})_2(S^2)_12$ (Table 1) for $x = 0$ and 0.3. These deviations can be explained by a small deviation of the Sn content from the stoichiometric value of 2 as small amounts of tin dioxide are observed on $^{119}$Sn Mössbauer spectra (see for instance Figure 3). With the latter assumption, we obtain the Sn content from the experimental values of $A^{2+}(x)$ values given in Table 1 and we get $(\text{Cu}^+)_{8}(\text{Fe}^{2+})_{0.75}(\text{Fe}^{3+})_{2.25}(\text{Sn}^{4+})_{1.94}(S^2)_{12}$ and $(\text{Cu}^+)_{8.3}(\text{Fe}^{2+})_{0.18}(\text{Fe}^{3+})_{2.52}(\text{Sn}^{4+})_{1.94}(S^2)_{12}$ for $x = 0$ and $x = 0.3$ respectively. Interestingly, the Sn content deviates similarly from 2 in both cases, namely by $\sim 0.06$ that we interpret by the existence of Sn vacancies. The amount of SnO$_2$ expected from this deviation is $\sim 3\%$ in agreement with the value observed for $x = 0$ (Figure 3).

The main feature of all $^{57}$Fe spectra is a central component, which consists apparently of two outer peaks and of an inner peak seen as a shoulder (Figure 4). The overall impression is that this central component remains essentially unchange d when $x$ varies. The latter component includes actually two doublets, i.e. four peaks labelled from 1 to 4 from negative to positive velocities. For $x = 0$, these four peaks have close areas so that two peak associations must be considered, on the one hand (1-2) and (3-4), and (1-4) and (2-3) on the other. The RT spectrum of Cu$_{8.5}$Fe$_{2.5}$Sn$_2$S$_{12}$ shows unambiguously that only the second is possible. From the hyperfine
parameters of Table 1, we are led to conclude that Fe\(^{3+}\) ions give rise to two different doublets for any value of \(x\). Their hyperfine parameters change little with \(x\) (Table 1).

Table 1: \(^{57}\)Fe hyperfine parameters: isomer shifts (IS) and quadrupole splittings (QS) for the various sites of Mössbauer spectra at 300 K and at 80 K. The bracketed relative area given for Fe\(^{2+}\) is equal to (1-2\(x\))/(3-\(x\)).

<table>
<thead>
<tr>
<th>Sulfides Cu(_{8-x})Fe(_x)Sn(<em>2)S(</em>{12})</th>
<th>Sites</th>
<th>IS mm.s(^{-1}) (±0.03)</th>
<th>QS mm.s(^{-1}) (±0.03)</th>
<th>Relative area % (±3)</th>
<th>IS mm.s(^{-1}) (±0.03)</th>
<th>EQ mm.s(^{-1}) (±0.03)</th>
<th>Relative area % (±3)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cu(_8)Fe(_3)Sn(<em>2)S(</em>{12}) ((x = 0))</td>
<td>Fe(^{2+})</td>
<td>0.59</td>
<td>2.88</td>
<td>23 (33)</td>
<td>0.71</td>
<td>3.01</td>
<td>25 (33)</td>
</tr>
<tr>
<td></td>
<td>Fe(^{3+})</td>
<td>0.40</td>
<td>0.18</td>
<td>34</td>
<td>0.52</td>
<td>0.18</td>
<td>38</td>
</tr>
<tr>
<td></td>
<td>Fe(^{3+})</td>
<td>0.29</td>
<td>0.48</td>
<td>42</td>
<td>0.39</td>
<td>0.50</td>
<td>36</td>
</tr>
<tr>
<td>Cu(<em>{8,3})Fe(</em>{2,7})Sn(<em>2)S(</em>{12}) ((x = 0.3))</td>
<td>Fe(^{2+})</td>
<td>0.60</td>
<td>2.80</td>
<td>7 (15)</td>
<td>0.69</td>
<td>2.92</td>
<td>7 (15)</td>
</tr>
<tr>
<td></td>
<td>Fe(^{3+})</td>
<td>0.43</td>
<td>0.20</td>
<td>26</td>
<td>0.42</td>
<td>0.20</td>
<td>25</td>
</tr>
<tr>
<td></td>
<td>Fe(^{3+})</td>
<td>0.31</td>
<td>0.44</td>
<td>67</td>
<td>0.31</td>
<td>0.44</td>
<td>68</td>
</tr>
<tr>
<td>Cu(<em>{8,5})Fe(</em>{2,5})Sn(<em>2)S(</em>{12}) ((x = 0.5))</td>
<td>Fe(^{2+})</td>
<td>0.35</td>
<td>0.16</td>
<td>47</td>
<td>0.31</td>
<td>0.44</td>
<td>68</td>
</tr>
<tr>
<td></td>
<td>Fe(^{3+})</td>
<td>0.29</td>
<td>0.48</td>
<td>53</td>
<td>0.31</td>
<td>0.44</td>
<td>68</td>
</tr>
</tbody>
</table>

The assumption that Fe\(^{2+}\) and Fe\(^{3+}\) occupy respectively the 2(a) and 4(i) sites in \((\text{Cu}^+)_8(\text{Fe}^{2+})(\text{Fe}^{3+})_2(\text{Sn}^{4+})_2(\text{S}^2)_12\) is incompatible with the existence of two different Fe\(^{3+}\) components with almost equal abundances. We can then propose that site 2(a) is occupied by 1 Fe\(^{3+}\) ion while site 4(i) is occupied by 1 Fe\(^{2+}\) and 1 Fe\(^{3+}\) cations. A similar remark holds for the other samples. This implies that the excess Cu ions in the hyper stoichiometric compounds are located on the 4(i) site.

From bond lengths\(^{23}\) and from Mössbauer hyperfine parameters\(^{25}\) in the sulfide Cu\(_8\)Fe\(_3\)Sn\(_2\)S\(_{12}\) (\(x = 0\)), it was concluded that the major cationic species are Cu\(^+\), Sn\(^{4+}\), Fe\(^{3+}\) and Fe\(^{2+}\) which leads to write its formula as \((\text{Cu}^+)_8(\text{Fe}^{2+})(\text{Fe}^{3+})_2(\text{Sn}^{4+})_2(\text{S}^2)_12\) with an ordered distribution of Fe\(^{3+}\) and Fe\(^{2+}\) in the mixed layers. Yamanaka and Kato\(^{25}\) reported that their \(^{57}\)Fe Mössbauer spectra are composed of two Fe doublets with an outer one due to ferrous ions and an inner one due to ferric ions. The intensity of the inner doublet is mentioned to be twice that of the outer doublet,
assuming that ferrous and ferric ions have identical Lamb-Mössbauer factors. Figure 4 shows outer “ferrous” doublets whose hyperfine parameters are similar to those reported by the latter authors. However, the inner central components of our $^{57}\text{Fe}$ Mössbauer spectra consist of more than one doublet and are satisfactorily fitted with two doublets. This conclusion is at variance with the statements of Yamanaka and Kato$^{25}$. As the $^{57}\text{Fe}$ Mössbauer spectra and velocity range information are not mentioned in their study, it is difficult to understand, if the inner component that they discussed, consists actually of one doublet or more. The FWHM of the inner lines of the bcc $\alpha$-Fe spectrum is 0.30 mm.s$^{-1}$ at room temperature in the study of Yamanaka and Kato while it is 0.23 mm.s$^{-1}$ in our case. Their conclusions might result from a lack of spectral resolution. Differences in the preparation processes of the investigated sulfides might also constitute an alternative explanation of the differences between $^{57}\text{Fe}$ Mössbauer spectra.

In summary, we conclude to the presence of small amounts of Sn vacancies in the investigated sulfides. In addition, the repartition of Fe$^{2+}$ and Fe$^{3+}$ on the 2(a) and 4(i) sites is found to differ from the classically assumed one.

### 3.3. Thermoelectric properties

The electrical resistivity plots versus temperature for the seven Cu$_{8+x}$Fe$_{3-x}$Sn$_2$S$_{12}$ compositions (Figure 5a) clearly show a crossover from a semi-conducting to a metallic-like behaviour with a decrease of the resistivity by almost three orders of magnitude at room temperature as the copper content increases from $x = 0$ to $x = 0.50$. Indeed, Cu$_8$Fe$_3$Sn$_2$S$_{12}$ is a semi-conductor with a resistivity of 745 mΩ cm at room temperature, whereas the hyper stoichiometric phase Cu$_{8.5}$Fe$_{2.5}$Sn$_2$S$_{12}$ evidences the best semi-metallic behaviour of the series with a resistivity of 2.75 mΩ cm at room temperature. Moreover the evolution of the resistivity values is quite continuous,
the semi-conducting character decreasing regularly from $x = 0$ to $x = 0.5$, leaving place beyond $x = 0.3$ to a metal-like behaviour. It is worth pointing out that copper hyper-stoichiometry was already shown to be a promising way to bring down the resistivity over the pristine phase in systems such as $\text{Cu}_{2+x}\text{Mg}_{1-x}\text{SnSe}_4$ and $\text{Cu}_{2+x}\text{Cd}_{1-x}\text{SnSe}_4$.

The evolution of the Seebeck coefficient versus temperature (Figure 5b) shows that they are all $p$-type materials with rather high $S$ values ranging from 310 to 100 $\mu$V/K at room temperature. As expected, the thermal evolution of $S$ is closely related to that of $\rho$. Indeed, for $x \leq 0.22$, $S$ decreases as $T$ increases, i.e. as $\rho$ decreases, whereas for $x \geq 0.3$, the opposite is observed. A nearly independent temperature behaviour for $x = 0.25$ is observed, suggesting that this chemical composition is close to the semi-conductor to metal-like transition in this system. Note that the $x = 0.22$ sample was synthesized in addition to the other samples to determine more precisely the composition window where the transition occurs. Moreover, $S$ decreases as $x$ increases in agreement with the crossover from the semiconducting to the metal-like behaviour observed from electrical resistivity. For the pristine sulfide $\text{Cu}_8\text{Fe}_3\text{Sn}_2\text{S}_{12}$, the Seebeck coefficient also decreases as $T$ increases in agreement with its semiconducting behaviour. Nevertheless, the $S$ value of this compound is smaller than that of the semi-conducting $x = 0.10$ phase, in spite of its higher resistivity.
Figure 5. Temperature dependence of (a) electrical resistivity, (b) Seebeck coefficient and (c) power factor in the Cu$_{8+x}$Fe$_{3-x}$Sn$_2$S$_{12}$ series.
Considering that the Sn$^{4+}$ cations cannot participate to the electrical conduction, due to the $4d^{10}$ nature of their orbitals, only Cu$^+$, Fe$^{2+}$ and Fe$^{3+}$ should be involved in the electrical conductivity of these materials. The high univalent copper content and the fact that the CuS₄ tetrahedra form a 3D-framework (Figure 1) strongly suggest that the p-type transport properties in this sulfide material are governed by the Cu(I)-S framework involving a hybridization of the Cu($3d^{10}$) and S($3p^4$) orbitals. In this model, the presence of hole carriers in the copper network, i.e. the mixed valence Cu$^{2+}$/Cu$^+$ is rigorously governed by the aforementioned equilibrium Cu$^{2+}$ + Fe$^{2+} \rightleftharpoons$ Cu$^+$ + Fe$^{3+}$ (1). In other words, we believe that in this material, the Cu-S framework forms the conducting electronic network, but that the Fe$^{3+}$/Fe$^{2+}$ species play the role of hole donors/acceptors (reservoirs) for the generation and optimization of electrical properties.

Presence of large amount of Fe$^{2+}$, as in the stoichiometric compound Cu₈Fe₃Sn₂S₁₂, tends to hinder the formation of Cu$^{2+}$ centres (hole carriers) by the capture of the hole carriers to form Fe$^{3+}$ species according to the equation Fe$^{2+}$ + h$^+$ $\rightleftharpoons$ Fe$^{3+}$ (2). This is in agreement with the Vant’Hoff and Lechatelier law considering the equilibrium (1). Indeed, the latter imposes that the presence of high Fe$^{2+}$ content tends to displace the equilibrium in order to increase the Fe$^{3+}$ content, as already discussed above. Consequently, we expect that the formation of “mobile Cu$^{2+}$ centres” in the structure will be smaller for this limit composition, leading to a high resistivity value, i.e. semi-conducting behaviour. For the hyper-stoichiometric sulfides Cu$_{8+x}$Fe$_{3-x}$Sn$_2$S$_{12}$, the Fe$^{2+}$ content is decreased continuously as $x$ increases up to $x = 0.50$ and consequently the equilibrium (1) tends to be displaced in the opposite direction. As a result, the content of Cu$^{2+}$ centres will tend to increase with $x$, leading to a metallic-like behaviour with the highest electrical conductivity for higher $x$ values. Note that additional hole carriers may also be created by cationic deficiency as observed on the Sn site by Mössbauer spectroscopy.
Figure 5c represents the thermal evolution of the power factor in the \( \text{Cu}_{8+x}\text{Fe}_{3-x}\text{Sn}_2\text{S}_{12} \) series. The pristine \( \text{Cu}_8\text{Fe}_3\text{Sn}_2\text{S}_{12} \) exhibits a PF value of \( 0.9 \times 10^{-5} \) W/m K\(^2\) at 300 K, which increases to \( 0.83 \times 10^{-4} \) W/m K\(^2\) at 635 K. The increase of the copper concentration provides high power factor, especially at higher temperatures, in relation with the decrease of the electrical resistivity. As example, \( \text{Cu}_{8.3}\text{Fe}_{2.7}\text{Sn}_2\text{S}_{12} \) sample exhibits a value of \( 4.36 \times 10^{-4} \) W/m K\(^2\) at 300 K and reaches a maximum of \( 6.2 \times 10^{-4} \) W/m K\(^2\) at 520 K.

The temperature dependence of the total thermal conductivity is given in Figure 6a. All of these materials present low \( \kappa \) values, ranging from 1.08 W/m K for \( \text{Cu}_8\text{Fe}_3\text{Sn}_2\text{S}_{12} \) to 1.74 W/m K for \( \text{Cu}_{8.4}\text{Fe}_{2.6}\text{Sn}_2\text{S}_{12} \) at \( T = 300 \)K. It is important to note that these low \( \kappa \) values are intrinsic to the complex crystal structure of stannoidite and absolutely not a consequence of either poorly densified samples (geometrical densities greater than 98 \%) or of the presence of secondary phases. For any copper content, the total thermal conductivity decreases monotonically with the increase of the temperature, leading to very low \( \kappa \) values at high temperature (\( \leq 1 \) W/m K). The electronic contribution \( \kappa_e \) to the thermal conductivity is calculated using the Wiedemann-Franz relation (\( \kappa_e = L_0\sigma T \)), while the lattice thermal conductivity \( \kappa_L \) is obtained after subtracting \( \kappa_e \) from \( \kappa \), according to the relation \( \kappa = \kappa_e + \kappa_L \). Figure 6b clearly shows that the lattice contribution to the thermal conductivity is dominant over the entire measured temperature range, even if it decreases monotonically when the temperature increases. As example, the \( \kappa_L \) value of the pristine phase decreases from 1.1 W/m K at 325 K to 0.68 W/m K at 635 K. This suggests that the decrease of the \( \kappa_L \) component is due to the increase of phonon-phonon scattering (Umklapp process). Such low lattice thermal conductivity values observed in this stannoidite phase could be due to mass contrast between \( \text{Fe}^{2+}/\text{Fe}^{3+} \) and \( \text{Cu}^+ \) with \( \text{Sn}^{4+} \) along with other effects such as those of point defects and strains. On the other hand, it is found that \( \kappa_L \) increases with \( x \). This
may be due to the progressive disappearance of the mixed valence Fe$^{2+}$/Fe$^{3+}$ on the Fe crystallographic sites when the copper concentration increases (i.e. decrease of the Fe$^{2+}$/Fe$^{3+}$ ratio from 1/2 in the pristine stannoidite to 0 for $x = 0.5$), which reduces the structural disorder in the lattice. Finally, it must be pointed out that the $\kappa_L$ values in the full series are also far below from those reported in related-stannite compounds (for example, $\kappa_L = 4.7$ W/m K at RT in Cu$_2$ZnSnS$_4$). Remarkably, it is in the same range as other copper based sulfide minerals such as pristine Cu$_{12}$Sb$_4$S$_{13}$ tetrahedrite$^{15}$ and Cu$_{26}$V$_2$Sn$_6$S$_{32}$ colusite.$^{18,38}$

Figure 6. Temperature dependence of (a) total thermal conductivity and (b) lattice thermal conductivity in the Cu$_{8-x}$Fe$_{3-x}$Sn$_2$S$_{12}$ series.
The dimensionless thermoelectric figure of merit $ZT$ versus temperature is shown in Figure 7. Copper to iron substitution significantly enhances the thermoelectric performance of stannoidite, leading to a maximum $ZT$ value of 0.35 at 630 K for the copper hyper-stoichiometric sample $x = 0.5$. The improvement here is nearly five fold over the pristine phase ($ZT = 0.07$ at 630 K). Such significant improvement in $ZT$ is mainly associated to the semi-conducting to metal-like behaviour crossover induced by copper hyper-stoichiometry and to the very low thermal conductivity of these materials, especially at high temperature.

Figure 7. Temperature dependence of the figure of merit $ZT$ in the $\text{Cu}_{8+x} \text{Fe}_{3-x} \text{Sn}_2 \text{S}_{12}$ series.

4. CONCLUSION

We have demonstrated that high purity and compact $\text{Cu}_{8+x} \text{Fe}_{3-x} \text{Sn}_2 \text{S}_{12}$ stannoidite bulk samples can be synthesized using mechanical alloying combined with spark plasma sintering. Besides the low cost and non-toxicity of the elements, this sulfide presents the advantage of a great flexibility for the optimization of its transport properties, by the control of the Cu content. Indeed, we have
shown that copper hyper-stoichiometry in stannoidite induces a drastic modification of its TE properties from a semiconducting poor TE ($ZT_{630 K} = 0.07$) state for the pristine phase ($x = 0$) to a semi-metallic attractive TE ($ZT_{630 K} = 0.35$) state for the richest copper phase ($x = 0.5$). The optimization of these performances is explained in the frame of the iono-covalent model of the chemical bonds, by varying the $\text{Fe}^{2+}/\text{Fe}^{3+}$ ratio leading to a semi-metallic behaviour with the highest conductivity for higher $x$ values. We have also shown that the thermal conductivity of these stannoidite compounds is relatively low due to its complex crystal structure with a large number of atoms in the unit cell and cationic sites. Moreover, even though the intrinsic substitution allows a huge improvement in the $ZT$ value over the pristine phase, it does not bring reduction in the lattice thermal conductivity, leaving large possibilities for further enhancements of the thermoelectric properties of stannoidite material by suitable substitutions.

We strongly believe that ternary/quaternary sulfides have to be more carefully investigated and revisited by controlling accurately the effect of doping upon their electrical and thermal properties, and developing innovative processes for reaching higher $ZT$ values.

Additional Note: At the end of this study, we learned of that a stannoidite type material with the only formula $\text{Cu}_{16}\text{Fe}_{4.3}\text{S}_{24}\text{Sn}_{4}\text{Zn}_{1.7}$ was revealed to exhibit thermoelectric properties with a $ZT$ factor of 0.22 at 623 K, supporting the great potential of this structural type for thermoelectric properties.
ASSOCIATED CONTENT

Supporting Information.

The following files are available free of charge.

- XRD pattern of ball-milled Cu$_8$Fe$_3$Sn$_2$S$_{12}$ powder (Figure S1, PDF)
- Rietveld refinement of XRD pattern of Cu$_{8.3}$Fe$_{2.7}$Sn$_2$S$_{12}$ (Figure S2, PDF)
- Crystallographic data for Cu$_{8+x}$Fe$_{3-x}$Sn$_2$S$_{12}$ (Table S1, PDF)
- Atomic coordinates for Cu$_{8+x}$Fe$_{3-x}$Sn$_2$S$_{12}$ (Table S2, PDF)

AUTHOR INFORMATION

Corresponding Author

*E-mail: emmanuel.guilmeau@ensicaen.fr

ACKNOWLEDGMENT

The authors would like to thank Christelle Bilot and Jérôme Lecourt for technical support and the financial support of the French Agence Nationale de la Recherche (ANR), through the program “Investissements d’Avenir” (ANR-10-LABX-09-01), LabEx EMC3.
REFERENCES


(4) Hsu, K. F.; Loo, S.; Guo, F.; Chen, W.; Dyck, J. S.; Uher, C.; Hogan, T.; Polychroniadis, E. K.; Kanatzidis, M. G. Cubic AgPb\textsubscript{m}SbTe\textsubscript{2+m} Bulk Thermoelectric Materials with High Figure of Merit. *Science* 2004, 303, 818–821.


(8) Xie, H.; Su, X.; Zheng, G.; Yan, Y.; Liu, W.; Tang, H.; Kanatzidis, M. G.; Uher, C.; Tang,
X. Nonmagnetic In Substituted CuFe\textsubscript{1-x}In\textsubscript{x}S\textsubscript{2} Solid Solution Thermoelectric. *J. Phys. Chem. C* **2016**, *120*, 27895–27902.


Figure 1. View of the crystal structure of stannoidite Cu$_8$Fe$_3$Sn$_2$S$_{12}$.

439x216mm (95 x 95 DPI)
Figure 2. Rietveld refinement of Cu8Fe3Sn2S12: as usual, red dots, black and blue curves represent the observed, calculated and difference plots, respectively. The green vertical lines represent the position of the Bragg reflections. Top lines are reflections of the stannoidite: short lines are $h,k,l=3n+1$ and $h,k,l=3n+2$ reflections while large lines are $h,k,l=3n$ reflections. Bottom lines are reflections of the SnO2 impurity. The inset shows the broadening of the $h,k,l$ reflections with $l=3n+1$ and $l=3n+2$ (white arrows) and the main reflection of the SnO2 impurity (black arrow).

60x47mm (300 x 300 DPI)
Figure 3. RT 119Sn Mössbauer spectrum of Cu8Fe3Sn2S12

142x125mm (300 x 300 DPI)
Figure 4. $^{57}$Fe Mössbauer spectra of Cu$_{8+x}$Fe$_{3-x}$Sn$_2$S$_{12}$ with x increasing from left to right (a) top row, at 300 K for x = 0, 0.3 and 0.5 and b) bottom row, at 100 K for x = 0 and 0.3
Figure 5. Temperature dependence of (a) electrical resistivity, (b) Seebeck coefficient and (c) power factor in the Cu$_{8+x}$Fe$_{3-x}$Sn$_2$S$_{12}$ series.
Figure 6. Temperature dependence of (a) thermal conductivity and (b) lattice thermal conductivity in the 
Cu$_{8+x}$Fe$_{3-x}$Sn$_2$S$_{12}$ series.
Figure 7. Temperature dependence of the figure of merit ZT in the Cu$_{8+x}$Fe$_{3-x}$Sn$_2$S$_{12}$ series.

189x175mm (299 x 299 DPI)