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Nuclear Spin Symmetry Conservation in $^1\text{H}_2^{16}\text{O}$ Investigated by Direct Absorption FTIR Spectroscopy of Water Vapor Cooled Down in Supersonic Expansion

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Abstract

We report the results of an experimental study related to the relaxation of the nuclear spin isomers of the water molecule in a supersonic expansion. Rovibrational lines of both ortho- and para- spin isomers were recorded in the spectral range of $\text{H}_2\text{O}$ stretching vibrations around 3700 cm$^{-1}$ using FTIR direct absorption. Water vapor seeded either in argon, helium or oxygen or in a mixture of oxygen and argon was expanded into vacuum through a slit nozzle. The water vapor partial pressure in the mixture varied over a wide range from 1.5 to 102.7 hPa, corresponding to a water molar fraction varying between 0.2 and 6.5%. Depending on expansion conditions, the effect of water vapor clustering was clearly seen in some of our measured spectra. The Boltzmann-plot of the line intensities allowed the $\text{H}_2\text{O}$ rotational temperatures in the isentropic core and in the lateral shear layer probed zones of the planar expansion to be determined. The study of the $OPR$, i.e the ratio of the ortho- to para- absorption line intensities as a function of $T_{\text{rot}}$, did not reveal any signs of the $OPR$ being relaxed to the sample temperature. In contrast, the $OPR$ was always conserved according to the stagnation reservoir equilibrium temperature. The conservation of the $OPR$ was found irrespective of whether water molecule clustering was pronounced or not. Also no effect of the paramagnetic oxygen admixture enhancing $OPR$ relaxation was observed.

Introduction

Water is an asymmetric top molecule, and its rovibrational levels are conventionally labelled by $J_{K_a,K_c}$, where $J$ is the total rotational angular momentum quantum number and $K_a$ and $K_c$ are quantum numbers of the components of the total angular momentum on the principal axes $a$ and $c$, respectively. These levels are assigned in the ground vibrational state to either para or ortho species for even or odd $K_a + K_c$, respectively. The notations are inverted in the antisymmetric vibrational stretch $\nu_3$ state.

The two hydrogen nuclei in a water molecule have either parallel or anti-parallel spins.
Similar to the hydrogen molecule, the conversion between these two forms is strictly forbidden in an isolated water molecule and strongly improbable in the gase phase. Water vapor can therefore, be thought to be a mixture of two stable spin-isomer forms: ortho and para. Para-isomers which have a total nuclear spin statistical weight \( g_{\text{NS}} \) equal to unity (\( g_{\text{NS}} = 2I + 1 \), where \( I \) is the total nuclear spin: \( I_{\text{para}} = 0, I_{\text{ortho}} = 1 \)) are dominant in \(^1\text{H}_2\text{O}\) water vapor at very low temperatures since the water molecule ground state belongs to the para sub-system of rotational energy levels. In contrast, thermal population of many rotational levels at elevated temperatures causes ortho-isomers to dominate in a mixture because of the higher nuclear spin statistical weight of ortho states. The limiting high temperature ortho-to-para ratio (\( OPR = 3 \)) of the nuclear spin isomer abundances is already reached at temperatures in excess of ca. 50 K and it remains constant at higher temperature, including, of course, room temperature. Some experimental studies (see e.g. \(^2\)) carried out on the supersonic cooling of water vapor seeded in Ar, relied on the assumption that \( OPR = 3 \) is preserved in the jet expansion.

An introduction to recent studies of nuclear spin isomer conversion in water vapor can be found in the paper from Manca Tanner et al.\(^3\) Much attention has been paid in the last few years (see e.g. refs 5-9) to the spectroscopic investigation of whether the normal \( OPR \) can be significantly distorted at near room temperature following multiple adsorption and desorption of water molecules onto the surface of various porous media such as adsorbent charcoal or polymer sorbents. Following initial observations dating back almost 30 years,\(^4\) there were more recent claims\(^5\) that an increase of \( OPR \) up to ten instead of three at near room temperature can be reached using a type of frontal gas-chromatograph column. Moreover, it was claimed in ref.\(^5\) that the non-equilibrium \( OPR \) ratio can be conserved over a long period (months) when a spin-isomer enriched sample is frozen. Once heated and released from the ice, the vapor is still in its non-equilibrium spin-isomer state. These experimental findings were then subject to a contradictory evaluation. There were attempts to reproduce experiments reported in ref.,\(^5\) which yielded either at least partially positive\(^6,7\) or entirely
negative\textsuperscript{1,8} results. To summarize, it can be stated nowadays that at least the idea of very slow spin-isomers conversion in the condensed phase has not met any independent confirmation and has to be ruled out. In contrast, it has been shown that ortho-para conversion in the condensed phase can occur on a timescale of between milliseconds\textsuperscript{9} and hours.\textsuperscript{10–13} In general, the results obtained in ref.\textsuperscript{5} were characterized e.g. in ref.\textsuperscript{3} as having a “nonstandard interpretation”. It was suggested in particular (see e.g.\textsuperscript{8,14}) that microwave radiation-induced desorption might be responsible for the effect observed in ref.\textsuperscript{4,5} and that no ortho-para enrichment occurred at all. This suggestion seems, however, unlikely since the experiments with a diode laser spectrometer\textsuperscript{7} apparently have confirmed the phenomenon of ortho-para enrichment detected previously in ref.\textsuperscript{5} with the use of a Backward Wave Oscillator (BWO).

The results reported in ref.\textsuperscript{3} showed a rapid change in the spin-isomer state in a supersonic expansion of $^1\text{H}_2^{16}\text{O}$ water vapor seeded in argon at a relatively high water molar fraction. Whereas at a low water vapor molar fraction ($0.35% < x < 0.9\%$) in a mixture with the carrier gas, the nuclear spin symmetry was conserved, at higher water molar fractions ($0.9\% < x < 1.6\%$) the OPR was seen to be completely relaxed, i.e. the measured OPR responded to a low rotational temperature in expansion. This fast relaxation cannot be explained by intramolecular processes in an individual water molecule and was thus interpreted as a result of water cluster formation which is able presumably to significantly facilitate nuclear spin conversion (NSC). The rapid transition from nuclear spin symmetry conservation to complete nuclear spin relaxation regimes within the narrow range of water mole fractions that was observed in ref.,\textsuperscript{3} has not found a clear explanation up-to-now. An attempt to reproduce the results reported in ref.\textsuperscript{3} was undertaken recently in ref.\textsuperscript{15} using a diode laser spectroscopic examination of two water vapor ortho- and para- absorption lines in an H$_2$O seeded in Ar expansion. Virtually no signs of nuclear spin relaxation was observed irrespective of whether the clustering in an expansion was definitely present or not. No correlation between clustering in the expansion and nuclear-spin isomerization was thus observed.
The idea of water clusters promoting the nuclear spin relaxation process that was put forward in ref., has much in common with an assumption made initially in ref. where preferred clustering of heavy D₂O water molecules from their ground ortho-state was first suggested. In their thorough recent study, Vilesov et al. assumed to have formed small water clusters predominantly made up of para-H₂O isomers using water embedded in an Ar matrix at low temperature. By waiting for 1400 minutes for the complete nuclear spin conversion of water molecules in the Ar matrix at 4 K, they produced nearly 100 % of para molecules in solid Ar because the mostly populated energetic level at the considered temperature, is the lowest rotational energy level of the para state (i.e. \( J_{K_aK_c} = 0_{00} \) state in the vibrational ground state). A fast warming up to 50 K of the matrix resulted in a rapid evaporation of Ar atoms, leaving behind water clusters on the cold substrate. The sublimation of such ice showed that the OPR of the molecules released into the gas phase was equilibrated at the high temperature limit. If we assume that the ice prior to the sublimation was a pure para-ice, the lifetime of para-H₂O in ice must be less than \(~ 30 \) min, a value which should be compared to a lifetime of a month, claimed in ref. The nuclear spin relaxation time in the gas-phase water dimer was estimated in ref. to exceed 3 ms. According to ref., rapid nuclear spin relaxation of the water dimer embedded in an Ar matrix is likely to occur on the time-scale of a few minutes. All these observations are invaluable for understanding the nature and the rate of nuclear spin conversion in various media including astrophysical environments. In the paragraphs below we shall address the above estimates while discussing the results of our experiments.

The present paper aims at further investigation of the water molecule nuclear spin symmetry conservation and relaxation in a supersonic expansion of \(^1\)H\(^{16}\)O water vapor seeded in argon, helium or in oxygen as carrier gases. Mid-infrared spectra were recorded using the Jet-AILES apparatus at the SOLEIL synchrotron facility.

The use of a supersonic jet cross-probed by an FTIR spectrometer has both advantages and disadvantages for the study of relaxation processes. On one hand, rapid adiabatic
cooling of the core part of the jet gives rise to a significant thermal non-equilibrium which can easily be observed in the high-resolution absorption spectra. Low values of the isentropic core rotational temperature result in a limited set of rotational levels being populated and consequently, only a small number of rotational lines can be seen in the spectrum. Also the formation of dimers and larger clusters in the cold part of a jet is clearly seen in the expansion of water vapor seeded in Ar as was evidenced e.g. in ref.\textsuperscript{18-20} The spectral shifts of the small cluster stretching bands were monitored in ref.\textsuperscript{18-20} as a function of successive solvation of pure water clusters by argon atoms. On the other hand, only fast relaxation processes can be studied in such an experimental geometry where the supersonic jet expanding from the slit reaches and crosses the IR beam in few microseconds.

The effect of lateral shock waves and viscous shear layers was taken into account. This effect leads to multi-temperature gas samples being probed at the same time. Thorough separation of spectral signatures into low-temperature and high-temperature ones was made by means of a Boltzmann plot for the measured absorption line intensities as described below. The use of a movable Pitot probe was used to characterize the supersonic expansion which was then used for FTIR spectroscopic observations. In spite of the presence of the small water cluster signatures in our obtained spectra, no transition to a nuclear spin relaxation regime was observed: the $OPR$ derived from the spectra was conserved on a level characteristic of equilibrium conditions in the stagnation reservoir, that is the $OPR$ was always equal to 3 irrespective of the extremely low rotational temperature. In addition, no change in $OPR$ was observed when the argon carrier gas was replaced by oxygen. The latter is known to enhance nuclear spin relaxation because of its associated magnetic moment.\textsuperscript{10,21,22} Based on the results obtained, we are in a position to dismiss the hypothesis of a water clustering effect on nuclear spin relaxation and to question the origin of the nuclear spin relaxation reported previously for a similar experiment.\textsuperscript{3}
Experimental set-up and recording of the spectra

Jet-AILES apparatus

The Jet-AILES apparatus was used to record the mid-infrared (MIR) spectrum of water vapor cooled down to a rotational temperature between 10 and 42 K in a supersonic expansion. This experimental set-up has already been described in detail in other studies. Briefly, a planar supersonic jet was formed by expanding water vapor admixed in various carrier gases (argon, helium, oxygen) from a high pressure reservoir (2 bar maximum) to a low pressure chamber through a slit nozzle (60 mm × 36 µm or 60 mm × 18 µm).

This chamber was evacuated by two Roots pumps (Edwards EH 500 and 2600) backed by a primary pump (Edwards GV80 Drystar), delivering an effective pumping speed of 1800 m³/h. The gas flow was probed with the modulated infrared (IR) light beam issuing from the rear parallel exit of the high-resolution interferometer (Bruker IFS 125HR) equipping the AILES beamline. The IR beam was focused into the gas expansion using a first set of gold coated mirrors with a magnification factor of 1.14. After its absorption by the cold expansion, the IR beam was collected and focused by a second set of mirrors onto a liquid-nitrogen cooled InSb detector connected to the interferometer. A combination of a CaF₂ beamsplitter and a tungsten lamp was chosen to investigate the OH stretching region located around 3700 cm⁻¹.

The spectra were recorded within the spectral range between 3400 cm⁻¹ and 3900 cm⁻¹ where strong absorption by water vapor ν₁ and ν₃ stretching bands can be detected. In high-resolution spectra (Figure 1) the number of intense rotational lines varies significantly as a function of rotational temperature. Despite the significantly good signal-to-noise ratio achieved, the noise level in high resolution spectra did not permit detection of the weak, broad and virtually structureless absorption bands which belong to water clusters. To examine the evolution of cluster content under various expansion conditions, it was necessary to repeat the measurements at a much lower instrumental resolution (1 cm⁻¹). Figure 2 shows that
cluster absorption does manifest itself in the region of free–OH vibrations as well as bonded–
OH vibrations as broad unresolved features accumulating contributions from (H₂O)ₙ and
(H₂O)ₙArₘ clusters presumably containing up to dozens of molecules.²⁰

Each experimental condition (see Table 1) was repeated twice: a first recording was
performed at high resolution (0.002 cm⁻¹, boxcar apodization, iris aperture: 0.8 mm) to
determine the rotational temperature and the OPR, while a second one was performed at low
resolution (1 cm⁻¹, triangle apodization, iris aperture: 0.8 mm) to track the presence of water
clusters. The aperture setting was kept unchanged for high and low resolution recordings
so that the dimensions of the infrared beam through the flow remain unchanged (see Figure
3). Note that the spectrometer was maintained under high vacuum (1.2 × 10⁻⁴ – 2.0 × 10⁻⁴
hPa) using a turbomolecular pump with active levitated magnetic bearings (Edwards model
1X455), thus minimizing the contribution of atmospheric water to the absorption spectra.

The continuous water vapor production was controlled by a vapor generation CEM-
system (Controlled Evaporation and Mixing, Bronkhorst, model W-303A) consisting of a
Coriolis liquid mass flow meter (mini Cori-Flow M12 Bronkhorst, ±0.2% of rate), a mass
flow controller (model F-202AV Bronkhorst, ±0.5% Rd plus ±0.1% FS) for the carrier gas
and a temperature controlled mixing and evaporation device. This system was used to vary
the mass flow rate of water vapor between 2 and 100 g/h. The flow rate of the carrier gas
was varied between 20 and 40 slm (1 standard liter per minute was measured at 0°C and 1
atm). The water vapor molar fraction was varied between 0.21% and 6.91%. This interval
was therefore larger than that corresponding to the former study reported in ref.³

To avoid water condensation, the inlet gas lines were wrapped in heating wires and main-
tained at the appropriate temperature of 40°C with a PID temperature controller. The gas
reservoir and the nozzle were made from a block of tempered aluminum. The temperature of
this element was regulated at 40°C with two heating cartridges and a second PID tempera-
ture controller. The pressure of the gas reservoir was measured using a bakeable capacitance
manometer (MKS Baratron 5000 Torr, model 615A) maintained at 100°C to avoid water
condensation into the gauge. The pressure of the expansion chamber was measured with a 100 Torr full scale range Baratron (MKS model 626A).

Structure of the supersonic expansion

The supersonic expansion produced by one of the slit nozzles (60 mm × 18 µm) was carefully characterized with a Pitot probe. For this purpose, the slit nozzle was placed in a different vacuum chamber, at the University of Rennes (France), evacuated by a set of powerful mechanical pumps (15,000 m³/h). A butterfly valve positioned between the vacuum chamber and the pumping unit was adjusted in order to match the pumping speed to that corresponding to the Jet-AILES apparatus (1800 m³/h). The Pitot probe measured impact pressures from which the Mach number of the flow could be extracted. It is constituted of a stainless steel capillary (Outer Diameter/Inner Diameter = 1.4/1.1 mm) connected to a capacitance manometer (MKS Baratron, 100 Torr) by a flexible tube. Its displacements in two perpendicular directions were controlled by two stepper motors with a precision better than 0.1 mm.

Figure 3 presents maps of various characteristics of the supersonic expansion of pure argon (20.1 slm), in a plane perpendicular to the long edge of the slit. The stagnation and residual pressures were 1072 and 0.68 hPa, respectively, thus very close to the conditions obtained with the Jet-AILES apparatus. Impact pressures measured by the Pitot probe are reported in this map, without any further treatment. It allows the diamond shock-cell pattern typical of an underexpanded free-jet expansion to be visualized. A succession of three supersonic cells each of about 20 mm long can be seen. The first cell (commonly known as the “zone of silence”) is terminated by the intersection of the two lateral shocks 20 mm downstream from the nozzle exit. The lateral extension of this cell is about 8 mm at its largest width. The trace of the IR beam is sketched on the figure. The optical axis was set at about 5 mm from the nozzle exit. The inner circle of about 1 mm in diameter corresponds to the spot focus, positioned at the middle of the slit aperture, while the outer ellipse delimits
the traces of the beam at the two edges of the slit. Part of the infrared beam impinges on the lateral shocks and viscous shear layers which are responsible for a deceleration and compression of the flow. This effect leads to the presence of rotationally “warm” molecules absorbing the IR light along its path that have to be taken into account for the analysis of spectra and to extract the rotational temperature of the water vapor in the cold part of the supersonic expansion.

The hydrodynamic characteristics of the first cell of the jet, delimited by the nozzle exit and the normal shock wave located at about 20 mm downstream, have been extracted from the Pitot probe measurements using the so-called Rayleigh formula. Strictly speaking, this procedure only applies within the assumption of continuous flows, i.e. flows characterized by a Knudsen number (Kn) lower than 0.01. Regarding the present approach, the Knudsen number can be defined as the ratio between the mean free path of the expanding molecules and the outer diameter of the Pitot probe. As displayed in Figure 3 (panel $b$), Kn attains a value of 0.125 just before the shock wave, which denotes a rarefied regime still far from the free molecular flow regime (Kn $> 10$). It seems appropriate therefore to use this means of characterization for our free jet expansion issuing from a very narrow width. Note that the values returned by the Rayleigh formula are not correct beyond the shock wave which is a source of entropy. The Mach number (Figure 3, panel $c$) attains values up to about 17 in the infrared probed zone, revealing an important enthalpy conversion into kinetic energy, thus yielding very low translational temperatures, as can be seen in panel $d$. The translational temperature is 3.4 K close to the optical axis, which is located at 5 mm downstream from the nozzle. The Pitot probe measurements have been compared to the isentropic model established on the basis of the method of characteristics. Calculated and measured temperatures are remarkably close, thus confirming the validity of the measurements returned by the Pitot probe. In the presence of water vapor, the translational temperature is expected to reach slightly higher values. Indeed, adding a polyatomic molecule in the carrier gas modifies the hydrodynamics by decreasing the specific heat ratio of the mixture and conse-
quently, the Mach number increase is smaller (some internal energy remains stored in the internal degrees of freedom of the water molecules). The main reason however, originates from thermodynamics: the condensation heat released by the clustering of water molecules is high and causes very significant warming of the flow, as can be seen from Table 1. Another important parameter of the flow field is its molecular density (Figure 3, panel e). As for the temperature, the molecular density drop associated with our free jet expansion is extremely abrupt, evolving from $1.7 \times 10^{19} \text{ cm}^{-3}$ at the nozzle exit to $3.4 \times 10^{16} \text{ cm}^{-3}$ at the optical axis location. It is therefore expected that most of the relaxation processes as well as cluster formation that rely on molecular collisions, occur mainly very close to the nozzle exit where the molecular density is still high.

The hydrodynamic time, denoted $\tau_{\text{hyd}}$ and defined as the time needed by the gas to reach the optical axis from the nozzle exit, can be easily estimated. In a free-jet, the gas reaches its limit velocity $v_\infty$ very rapidly downstream from the nozzle, i.e. after covering a distance equivalent to only a few slit widths. The limit velocity corresponds to a complete conversion of the enthalpy of the gas into kinetic energy (Mach number $M \to \infty$; flow temperature $T \to 0 \text{ K}$) and it is then easily retrieved from the conservation of energy equation:

$$v_\infty = (2c_p T_0)^{1/2},$$

where $c_p$ is the heat capacity at constant pressure of the carrier gas, and $T_0$ is the stagnation temperature, fixed at 313 K in the present study. The value obtained for a flow of argon is 570 m/s, which is remarkably close to the value of 558 m/s calculated from the Mach number and the temperature extracted from the Pitot probe measurement ($v = aM$, where $a = \sqrt{\gamma r T}$ is the speed of sound, $\gamma$ is the specific heat ratio and $r$ is the specific gas constant), thus validating the $T \to 0 \text{ K}$ approximation. Hence the hydrodynamic times associated with helium, oxygen and argon are 2.8, 6.6 and 8.8 microseconds, respectively. These values are slightly overestimated as the heat of water condensation released in the flow adds a supplement of enthalpy into the flow which can be converted into additional kinetic energy. One should keep in mind that these hydrodynamics times are smaller by several orders of magnitude than the timescale of milliseconds relative to ortho-para conversion in
Water clustering

Figure 2 shows that the rotational temperature steadily increases as the water vapor molar fraction increases in the expansion. This can be understood in terms of the progressive clustering of water molecules that results in a release of more latent heat when a more notable portion of a gas in a mixture condenses. The rotational temperature achieved by the water molecules in the expansion is not only governed by the condensation process. The specific heat ratio of the carrier gas is also an important parameter to consider as it defines the Mach number evolution of the expanding flow for a given nozzle geometry. Thus compared to a monoatomic gas expansion, the expansion of a diatomic gas is characterized by a lower cooling rate (i.e. a smaller Mach number increase) and therefore by a higher translational temperature. The rotational temperature of the water molecules is obviously limited by the “translational bath”. As an example, the rotational temperature achieved during our measurements in an expansion of pure oxygen was 31.2±0.6 K whereas no water clustering was detected on the low resolution spectrum. For completeness, it should be noted that the rotational relaxation phenomenon depends on the stagnation pressure and the nature of the collision partner. In this respect, helium is far less efficient than argon for inducing R–T energy transfer. Moreover, as the rotational relaxation is proportional to $P_0 d^*$ (see e.g. ref.27), where $P_0$ is the stagnation pressure and $d^*$ the slit width, a large stagnation pressure is required for efficient relaxation. However, as helium is lighter than argon by a factor of 10, the same molar flow of helium would lead to a stagnation pressure of about $\sqrt{10} \approx 3$ times lower than for argon. For these reasons (low R–T energy transfer and low stagnation pressure), the use of helium was rejected in favor of argon. As an example, the maximum flow rate tolerable by our pumping unit (30 slm) was used to inject helium together with a very small amount of water (0.28%), leading to a rotational temperature around 42 K. As
for oxygen, no water clustering was observed.

The extent of water clustering was estimated by comparing the water monomer density measured in the cold region of the jet to the monomer density calculated assuming no clustering. The way the monomer density was extracted from our high resolution absorption spectra is explained in detail in the next section, while the calculation was performed using the standard isentropic model equations. More explicitly, the local molecular density $N_{\text{jet}}$ of the flow is expressed as a function of the Mach number:

$$\frac{N_{\text{jet}}}{N_0} = \left(1 + \frac{\gamma - 1}{\gamma} M^2\right)^{\frac{1}{\gamma - 1}},$$

where $N_0$ is the total molecular density in the reservoir. For a free-jet expansion, the Mach number is modeled using the following analytical expression:

$$M = \delta^{\frac{\gamma - 1}{2}} \sum_{i=0}^{i=3} \frac{A_i}{\delta^i}.$$  \hfill (2)

Here $\delta = x/d^*$ is the dimensionless distance from the nozzle exit. The various $A_i$ coefficients can be found in ref.28. The calculated water monomer density is given by $x_{\text{H}_2\text{O}} N_{\text{jet}}$. As shown in Figure 4, water condensation reaches 80\% when argon is used as carrier gas, revealing therefore, an intense water clustering.

**Extraction of the rotational temperature from spectroscopic data**

Our aim was to determine the behaviour of the $OPR$ under various experimental conditions. The use of high resolution (0.002 cm$^{-1}$) makes it possible to accurately fit the observed line profiles and retrieve the fractional populations relative to the rotational energetic levels of the ortho- and para- molecules. It is then currently possible to determine the rotational temperature $T_{\text{rot}}$ of the molecules in the line-of-sight of the IR light beam. To take into account
instrument effects inherent to the Fourier Transform spectroscopic technique, we analysed the so-called experimental spectral absorptance (sometime called spectral absorption) denoted $\alpha(\tilde{\nu})$ as per the recommendation of IUPAC. Under that in our experimental conditions, layers of hot gas surround the cold gas and contribute significantly to the total absorptance of the IR light. In the limit of our experimental accuracy, we extracted the integrated Napierian absorbance associated with the two gaseous zones assuming that the medium can be described by a simplified warm/cold bi-modal model. Analysis of the rotational populations allowed us to estimate a rotational temperature for the warm gas and for the cold gas. The relative integrated absorbances obtained for 4 ortho lines and 1 para line in the cold gas allow to explore the behaviour of the OPR of water within the fast slit-jet expansion. In the following, we describe the procedure used to retrieve the parameters characterizing the cold part of the expansion.

The absorptance $\alpha(\tilde{\nu})$ is obtained by comparing the spectral intensity of light $I(\tilde{\nu})$ at the output of the chamber to the intensity of light at its entrance $I_0(\tilde{\nu})$:

$$\alpha(\tilde{\nu}) = \frac{\Delta I(\tilde{\nu})}{I_0(\tilde{\nu})} = \frac{(I_0(\tilde{\nu}) - I(\tilde{\nu}))}{I_0(\tilde{\nu})}.$$  \hspace{1cm} (3)

$I(\tilde{\nu})$ follows the Beer-Lambert law and is given by:

$$I(\tilde{\nu}) = I_0(\tilde{\nu}) \exp(-A_{fi} \times V(\tilde{\nu})),$$  \hspace{1cm} (4)

where $A_{fi}$ is defined as the integrated Napierian absorbance of the line for a transition from a state $i$ to a state $f$ and $V(\tilde{\nu})$ is a normalized line profile (generally a Voigt profile taking into account inhomogeneous Doppler broadening and homogeneous collisional broadening). $A_{fi}$ is given by the following equation:

$$A_{fi} = \int \sigma(\tilde{\nu}) N L d\tilde{\nu},$$  \hspace{1cm} (5)
where $\sigma(\tilde{\nu})$ is the absorption cross-section at the wavenumbers $\tilde{\nu}$, $L$ the thickness of the sample, $N$ is the number of molecules per unit volume. Then, one has

$$A_{fi} = S_{fi}^N NL,$$

(6)

where integrated absorption cross section of the line (also called line intensity in ref$^{32,33}$) $S_{fi}^N$ (cm$^{-1}$/molecule cm$^{-2}$) is given in the gas phase by:

$$S_{fi}^N = \frac{8\pi^3}{3hc} \tilde{\nu}_{fi} \left[ 1 - \exp \left( -\frac{hc\tilde{\nu}}{kT} \right) \right] \times \Re_{fi} \times 10^{-36} \times n_i,$$

(7)

where $T$ is the temperature, $\Re_{fi}$ (Debye$^2$) the square of the transition moment and $n_i$ represents the fractional population in the initial state. At low temperature (below 296 K), the wavenumber $\tilde{\nu}_{fi}$ of the transition is sufficiently high so that the exponential term vanishes. Then,

$$S_{fi}^N = \frac{8\pi^3}{3hc} \tilde{\nu}_{fi} \times \Re_{fi} \times 10^{-36} \times n_i.$$

(8)

Finally the integrated Napierian absorbance is related to the fractional population through the simple relation:

$$A_{fi} = F_{fi}^N NL \times n_i,$$

(9)

where $F_{fi}^N$ is independent of the temperature and afterwards will be called the line strength.

The evolution of the integrated Napierian absorbance is then directly related to the evolution of the population in the initial state. When the fractional populations of the rotational energy levels follow the thermodynamic equilibrium statistics, the population $n_i$ is given by:

$$n_i = \frac{1}{Q(T)} g_i \exp \left( -\frac{hcE_i}{kT} \right)$$

(10)

where the energy of the initial level $E_i$ is given in cm$^{-1}$ and $T$ in K, and $Q(T)$ is the partition function, $g_i = g_{NS} g_J$ with $g_{NS}$ is the degeneracy of the considered Nuclear Spin state and
\( g_J = 2J + 1 \) is the degeneracy of the rotational state (Zeeman sub-levels).

By extracting the integrated Napierian absorbance of the lines \( A_{fi} \) under our experimental conditions, it is then possible to extract the rotational temperature \( T_{\text{rot}} \) using the following linear equation:

\[
\log \left( \frac{A_{fi}}{F_{fi}^N/g_J} \right) = \log \left( \frac{N Ln_i/(2J+1)}{g_J} \right) = -\frac{hc}{k} \frac{E_i}{T} + \log \left( \frac{g_{NS}}{Q(T)} \right) \tag{11}
\]

which becomes

\[
\log \left( \frac{N Ln_i/(2J+1)}{g_J} \right) = -\frac{E_i}{T} + \log \left( \frac{g_{NS}}{Q(T)} \right) \tag{12}
\]

when the initial energy \( E_i \) is expressed in Kelvins.

In the spectral region around 3700 cm\(^{-1}\), the Doppler Half Width at Half Maximum (HWHM) ranges between \( 1 \cdot 10^{-3} \) and \( 5 \cdot 10^{-3} \) cm\(^{-1}\) for temperatures between 10 and 250 K. It is then necessary to take into account the width of the apparatus function to accurately model the line shape. The width of the apparatus function (\( \approx 2 \cdot 10^{-3} \) cm\(^{-1}\)) has to be taken into account to perform accurate analysis of the line shape. Experimentally, the intensity of the light is given by the convolution product:

\[
I_{\text{exp}}(\tilde{\nu}) = I(\tilde{\nu}) \ast f_{\text{app}}(\tilde{\nu}) \tag{13}
\]

where the apparatus function \( f_{\text{app}}(\tilde{\nu}) \) is modelled by the Fourier transform of the Boxcar function:

\[
f_{\text{app}}(\tilde{\nu}) = 2 \frac{1}{R} \times \text{sinc} \left( \frac{2\tilde{\nu}}{R} \right). \tag{14}
\]

Here \( \text{sinc}(x) = \frac{\sin(\pi x)}{\pi x} \). The resolution \( R \) is given by \( R = 1/MOPD \) where MOPD is the Maximum Optical Path Difference. In our case, the resolution corresponds to the resolution defined by the Bruker company divided by 0.9, then \( R = 2.22 \cdot 10^{-3} \) cm\(^{-1}\). The experimental absorption becomes:

\[
\alpha_{\text{exp}}(\tilde{\nu}) = \frac{(I_0(\tilde{\nu}) - I(\tilde{\nu})) \ast f_{\text{app}}(\tilde{\nu})}{I_0(\tilde{\nu}) \ast f_{\text{app}}(\tilde{\nu})} \tag{15}
\]
For FTIR spectroscopy, the entrance intensity $I_0(\tilde{\nu})$ is spectrally broad compared to the width of the apparatus function. Then, $I_0(\tilde{\nu}) \ast f_{\text{app}}(\tilde{\nu}) \approx I_0(\tilde{\nu})$ and the absorptance is given by:

$$\alpha_{\text{exp}}(\tilde{\nu}) = \frac{(I_0(\tilde{\nu}) - I(\tilde{\nu})) \ast f_{\text{app}}(\tilde{\nu})}{I_0(\tilde{\nu})} \approx \alpha(\tilde{\nu}) \ast f_{\text{app}}(\tilde{\nu})$$  \hspace{1cm} (16)

then

$$\alpha_{\text{exp}}(\tilde{\nu}) = (1 - \exp(-A_{fi} \times V(\tilde{\nu}))) \ast f_{\text{app}}(\tilde{\nu})$$  \hspace{1cm} (17)

The variations of absorption lines intensities have been plotted as a function of $T_{\text{rot}}$ for a series of reference lines listed in Table 2.

Since the gas temperature in the shear layers is significantly higher than in the central part of the jet, more observed rotational lines are due to absorption by the warm gas than by the cold one. We performed the analysis of the individual lineshapes based on a two-steps procedure which uses a homemade computational code written in MATLAB language:

(i) In the first step, the absorption $\alpha_{\text{exp}}(\tilde{\nu})$ of each individual line was fitted using a Gaussian profile $V(\tilde{\nu})$. The only fitted parameters were the integrated Napierian absorbance $A_{fi}$ and the HWHM of the Gaussian profile. For experimental conditions relative to higher water concentrations, contribution from the low temperature gas could be neglected for transitions originating from an initial energetic level higher than 190 K. Indeed for these transitions, the lineshape was perfectly fitted using Eq. 15 and the rotational diagram shows a linear behaviour for energy $E_i$ above 190 K (see Figure 5). Application of Eq. 9 yielded the averaged column density $N_L^{\text{hot}}$ listed in Table 1 for each line. It should be noted that for the calculation of the population factor $n_i$ appearing in Eq. 9, the $OPR$ value was assumed to be close to 3. Because of the high temperature considered here, this value is justified by the fact that calculations give values close to 3 irrespective of the nuclear spin equilibration dynamics (fast or slow nuclear spin conversion; see text below and Eqs. 17–21). Application of Eqs. 11-12 to the same integrated absorbances, led to the rotational temperatures $T_{\text{hot}}$, also listed in Table 1. For the case of a flow of 100 g/h of water in 30 slm of Ar, the
rotational diagram gives a high rotational temperature $T_{\text{hot}} = 251 \pm 11$ K very close to the translational temperature $T = 260 \pm 40$ K extracted from the HWHM Gaussian lineshape. For the “low temperature” lines, the difference between the calculated and experimental spectral absorptance shows a typical residue presented in Figure 6.a (case of the $1_{11} \leftarrow 1_{10}$ transition). For the case of low water concentration, our signal-to-noise ratio was too low to permit detection of high-$J$ rotational lines. Therefore the only observable transitions were those originating from initial energy states $E_i$ lower than 190 K. The rotational diagrams for ortho and para were linear for energy lower than 190 K. This means that the populations followed a Boltzmann distribution allowing us to extract rotational temperatures directly using Eq. 12. The rotational temperatures extracted for the ortho and para molecules are listed in Table 1.

(ii) In a second step, we focused our analysis on spectra recorded with higher water concentration. We fitted the lines corresponding to transitions related to initial rotational states below 190 K, including the contribution of the warm gas. The absorptance was then fitted using:

$$\alpha_{\text{exp}}(\tilde{\nu}) = \left(1 - \exp \left(-A^\text{cold}_{fi} \times V^\text{cold}(\tilde{\nu}) - A^\text{hot}_{fi} \times V^\text{hot}(\tilde{\nu}) \right) \right) \times f_{\text{app}}(\tilde{\nu}) \quad (18)$$

The Figure 6.b shows that the discrepancies between the calculated and the experimental absorptances are drastically reduced for a flow of 100 g/h of water in 30 slm of Argon. The only parameters in this second step were $A^\text{cold}_{fi}$ and the HWHM of the Gaussian profile $V^\text{cold}(\tilde{\nu})$. In this extreme case, the contribution of the hot molecules counts for a third of the total absorbance. We were then able to remove the hot gas contribution from the absorbance of these low-$J$ rotational lines. Figure 5 shows that the populations reported for the cold molecules in the rotational diagram follow a straight line.

In all cases, rotational temperatures for ortho and para subsystems were determined independently and were found to be nearly equal (see Table 1). The integrated absorbances obtained for the “cold” transitions and the average rotational temperatures in the various
experimental conditions are listed in Table 3. The Figures 7, 8, 9 and 10 show the evolution of the otho/para relative absorbances for several transitions as a function of rotational temperature. As these ratios indicate that the OPR has not been relaxed during the cooling down, we calculated the $n_i$ fractional population using a conversion factor $(CF)_{\text{slow}}$ as described by Eq. 23. The $NL^{\text{cold}}$ column densities estimated for the cold gas in various conditions are reported in Table 3 and can be compared to the warm gas contribution $NL^{\text{hot}}$. They have been used to estimate the fraction of condensed water.

Finally, we evaluated a possible contribution of homogeneous collisional broadening under the conditions of pressure and temperature of our experiment using the broadening coefficients tabulated in the HITRAN database.$^{32}$ Under the various experimental conditions used in this work, the collisional width was always less than $10^{-7}$ cm$^{-1}$ (HWHM), justifying a posteriori the use of a Gaussian profile for the lineshape analysis.

Although the infrared light beam diameter is rather large compared to the flow field dimension, two well defined low- and high-rotational temperatures could be extracted from our spectra using the above two-steps procedure, which seems contradictory regarding the density and temperature gradients highlighted by the Pitot probe measurements (see Figure 3). In the zone of silence, it appears that beyond a certain distance from the nozzle, the gas absorption becomes too weak to contribute significantly. Another assumption is that the rotational temperature no longer relaxes beyond a certain distance from the nozzle, due to a lack of collisions.

Discussion

To investigate the behaviour of the nuclear spin isomers spin species after the fast expansion, we followed the procedure used by Manca Tanner et al.$^3$ As the experimental data showed that rotational populations of ortho and para molecules were equilibrated at the same rotational temperature $T$ we conducted our analysis of the OPR using the following method.
The ratio of integrated absorbance of one ortho $f_i$ transition to one para $f_i'$ transition is proportional to the ratio of the fractional population of molecules in the two considered rotational states:

$$\frac{A_{f_i}}{A_{f_i'}} = \frac{F_{N_{f_i}}}{F_{N_{f_i'}}} \times \frac{n_i}{n_{i'}} = \frac{F_{N_{f_i}}}{F_{N_{f_i'}}} \times \frac{g_i}{g_{i'}} \exp \left(-\frac{\hbar c(E_i - E_{i'})}{kT}\right) \times CF$$

$$\frac{A_{f_i}}{A_{f_i'}} = \frac{F_{N_{f_i}}}{F_{N_{f_i'}}} \times \frac{g_{NS_i} g_{J_i}}{g_{NS_{i'}} g_{J_{i'}}} \exp \left(-\frac{\hbar c(E_i - E_{i'})}{kT}\right) \times CF$$

(19)

where $g_{NS} = 2I + 1$ is the nuclear spin states degeneracy given for a value of the total nuclear spin momentum number $I$ and $CF$ is a Conversion Factor.

$OPR$ is a key parameter for our analysis. The $OPR$ at a temperature $T$ can be defined assuming that the ortho and para molecules behave as independent species (however both in contact with the same thermal bath of the expanding gas). It can be calculated from separate partition functions evaluated for each nuclear spin conformers $Q_{ortho}(T)$ and $Q_{para}(T)$ expected at thermal equilibrium. When the $OPR(T)$ is out of equilibrium but the rotational ortho and para sub-systems are equilibrated, the coefficient of proportionality between the total ortho fractional populations $n_{ortho}$ and $Q_{ortho}(T)$ is different of the one between $n_{para}$ and $Q_{para}(T)$. The CF conversion factor in Eq. 19 is then given by : 

$$OPR(T) = \frac{Q_{ortho}(T)}{Q_{para}(T)} \times CF = \frac{\sum g_{NS}(ortho) g_{J}(ortho) \exp(-\frac{\hbar cE_{ortho}}{kT})}{\sum g_{NS}(para) g_{J}(para) \exp(-\frac{\hbar cE_{para}}{kT})} \times CF$$

(20)

Here and below the summation extends to all the ortho or para lines, respectively. Two limiting cases can be distinguished.

(i) In the case of Fast Nuclear Spin Conversion (designated by Fast in the following), the equipartition of the nuclear spin states gives a $(CF)_{Fast}$ factor equal to 1. As a result, equation (20) becomes:

$$OPR(T) = 3 \frac{\sum g_{J}(ortho) \exp(-\frac{\hbar cE_{ortho}}{kT})}{\sum g_{J}(para) \exp(-\frac{\hbar cE_{para}}{kT})}$$

(21)
(ii) In the case of Slow Nuclear Spin Conversion (Slow in the following), we assume that the total number of molecules in each nuclear spin configuration remains constant during the cooling. Starting from a gaseous mixture with an OPR of 3, the ratio of the absorbances has to be calculated with a temperature dependent \((CF)_{\text{Slow}}\) parameter imposing an \(OPR(T) = 3\) irrespective of the temperature:

\[
OPR(T) = 3 \times \left( \frac{\sum g_J(ortho) \exp(-\frac{hcE_{ortho}}{kT})}{\sum g_J(para) \exp(-\frac{hcE_{para}}{kT})} \right) = 3 \tag{22}
\]

thus giving

\[
(CF)_{\text{Slow}} = \frac{1}{\left( \frac{\sum g_J(ortho) \exp(-\frac{hcE_{ortho}}{kT})}{\sum g_J(para) \exp(-\frac{hcE_{para}}{kT})} \right)} \tag{23}
\]

\((CF)_{\text{Slow}}\) is calculated using equation (23) to determine the theoretical ratio \(A_{fi}/A_{f'j'}\) between absorbances of two transitions in the case of Slow NSC. In the section below, we shall compare the measured ratios of integrated absorption for selected pairs of \(ortho\)- and \(para\)-transitions with what can be expected for the limiting Fast or Slow nuclear spin conversion cases.

The theoretical ratio of integrated absorbances \(A_{fi}/A_{f'j'}\) was calculated using the relationship (19) into which the CF parameter was substituted either assuming it equals 1 in the case of Fast conversion or equation (23) in the case of Slow conversion. The values of \(J\) quantum number, the energy of the low lying level of a selected transition and the line intensities \(S_{fi}^N(296K)\) were taken from HITRAN database.\(^{32}\) Note that the line strengths \(F_{fi}\) that enter formula (19) were calculated from line intensities \(S_{fi}^N(296K)\) reported in Table 2. The error is between 5 and 10 % which gives an uncertainty of 10-20 % on the relative absorbances.

Then the calculated values of \(A_{fi}/A_{f'j'}\) were compared with the ratio of absorbances retrieved from the fit of experimentally recorded line profiles and given in Table 3. Comparison between experimental measurements and expected values are presented in Figures 7, 8, 9 and 10. Confidence domains presented in these figures for the theoretical values in case of Fast...
or Slow NSC are calculated using 10% error given by the uncertainties on line intensities $S_{fi}^N(296K)$ reported in the HITRAN Database.\textsuperscript{32}

Figures 7, 8, 9, and 10 show that in all cases, our measured ratios of integrated absorbances are in agreement with an assumption of Slow NSC. It is seen that even the use of oxygen instead of argon as a carrier gas, does not result in the change of the nuclear spin conversion rate. We do not observe any effect of cluster formation on the change in the nuclear spin conversion rate as was suggested in ref.,\textsuperscript{3} despite clear evidence of cluster signatures in our recorded low resolution spectra and an important fraction of condensed water molecules, as estimated from our high resolution spectra. The rate of water condensation in an expansion of argon was estimated by comparing the monomer concentration extracted from the line absorbances to the value given by the isentropic model for which a total absence of condensation is assumed. As shown in Figure 4, water condensation reaches 80% when argon is used as the carrier gas, revealing therefore, intense water clustering. Under our experimental conditions, a fast nuclear spin conversion would then be expected even at low temperature when the two models give very different ortho/para intensity ratios. Figures 7, 8, 9, and 10 show that such an effect does not occur. One explanation could arise from the expansion dynamics differing between our study and that performed by Manca Tanner et al.\textsuperscript{3} At first glance, the differences are quite subtle. Indeed, the flow characteristics in the isentropic part of a supersonic expansion are governed by only a few parameters linked to the nozzle geometry and the stagnation conditions (namely temperature, pressure, specific heat ratio of the expanding mixture, water molar fraction). It appears that in both studies, a slit nozzle has been used, argon was mainly used and very similar stagnation pressures and temperatures have been set, so that very similar flow expansions are therefore expected. One has to notice however, that the wider 100 µm width nozzle used in ref. 3 (versus 18 and 36 µm in the present work) certainly leads to a slightly lower cooling rate. However, as in this former study the flow was probed farther from the nozzle exit (10 mm vs 5 mm), the temperature and molecular density reached by the flow for equivalent gas compositions are
expected to be very similar to those obtained in the present work. However, it is interesting to notice that the extracted rotational temperature is systematically higher by about 5 K for equivalent partial pressures of water (see table 6 of ref. 3). One explanation could be attributed to a more pronounced water condensation induced by the wider slit nozzle used in ref. 3. Finally, to be complete, one has to point out, a hydrodynamic time (as defined previously) two times larger in ref. 3 ($\sim 18 \mu s$ vs $\sim 9 \mu s$) because of the larger probing distance. We are considering using a Laval nozzle to better control water clustering and to increase the hydrodynamic time (see e.g. ref. 35). It would provide us with new insights on the effects of the hydrodynamic time and the rate of water condensation in the expansion.

**Conclusion**

The present paper was aimed at a further examination of water vapor nuclear spin-isomerization. In recent years the mechanism and the effectiveness of nuclear spin conversion among water vapor ortho- and para- spin isomers have been the subject of a number of studies that often gave rise to contradictory conclusions. We have conducted a Jet-FTIR examination of several water vapor absorption lines seen in H$_2$O seeded expansions using pure argon or helium as carrier gases. Some experiments were carried out with dioxygen as carrier gas or co-added to expanding mixture of gases in order to accelerate ortho-para conversion due to collisions with paramagnetic oxygen molecules. To summarize, we did not observe any signs of nuclear spin relaxation in the wide range of expansion conditions which were used:

- H$_2$O molar fraction: from 0.2% to 6.5%;
- rotational temperature range: from 10 K to 42 K;
- transitions explored: one para line ($l_{01} \leftarrow 0_{00}$) and four ortho lines ($2_{02} \leftarrow 1_{01}; 0_{00} \leftarrow 1_{01}; 1_{11} \leftarrow 1_{10}; 2_{11} \leftarrow 1_{10}$).

In any event the measured OPR corresponded to the temperature in the stagnation
reservoir and was not relaxed to very low rotational temperatures measured at the sampled volume of the jet. Moreover, in spite of clear signatures of water clusters which were formed at some experimental conditions, we did not observe any effect of clustering on the rate of nuclear spin isomer conversion. This result agrees with a conclusion that has been drawn from a similar experiment in ref.\textsuperscript{15} and differs significantly from what has been reported previously by ref.\textsuperscript{3} Based on the results obtained, we are in a position to state that at least the suggestion of ref.\textsuperscript{3} that the transition from nuclear spin conservation to nuclear spin relaxation regimes is due to clustering in an expansion, is not supported by our measurements, also in agreement with the previous work.\textsuperscript{15}

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Table 1: Experimental conditions

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<th>Carrier gas</th>
<th>H₂O</th>
<th>P₁H₂O</th>
<th>P₂H₂O</th>
<th>P₃ch</th>
<th>dₚ</th>
<th>T₂rot (O/P)</th>
<th>NLcold</th>
<th>T_hot</th>
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<td>hPa</td>
<td>hPa</td>
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<td>10¹⁴</td>
<td>K</td>
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*a* water vapor/carrier gas molar ratio; *b* stagnation pressure; *c* residual pressure in the expansion chamber; *d* nozzle width (the slit length is 60 mm); *e* rotational temperature extracted from ortho (O) or para rovibrational lines (P); *f* column densities for hot and cold gases (see text for details); *g* rotational temperature of the warm residual gas in shear layers; *h* hydrodynamic time; *i* fraction of condensed water vapor.
Table 2: Assignments and some parameters of the H_2O absorption lines of the ν3 band used in this work

<table>
<thead>
<tr>
<th>Transition</th>
<th>Spin-isomer</th>
<th>Line position, a ( \text{cm}^{-1} )</th>
<th>Lower energy level, a ( \text{cm}^{-1} / \text{K} )</th>
<th>Line Intensity ( 10^{-19} S_{fi}^{N} ) ( \text{cm}^3/\text{mole} )</th>
<th>Line Strength, ( 10^{18} F_{fi}^{N} ) ( \text{cm}/\text{mole} )</th>
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<td>23.7944/34.2351</td>
<td>2.312</td>
<td>5.03633</td>
</tr>
<tr>
<td>2_11 ← 1_10</td>
<td>ortho</td>
<td>3807.01357</td>
<td>42.3717/60.9638</td>
<td>1.562</td>
<td>3.72412</td>
</tr>
<tr>
<td>3_13 ← 2_12</td>
<td>ortho</td>
<td>3816.09164</td>
<td>79.4964/114.3783</td>
<td>2.312</td>
<td>3.96143</td>
</tr>
<tr>
<td>2_20 ← 1_01</td>
<td>ortho</td>
<td>3863.31982</td>
<td>23.7944/34.2351</td>
<td>0.0456</td>
<td>0.09933</td>
</tr>
</tbody>
</table>

\( a \) - From ref. 32
Table 3: Rotational temperatures $T_{\text{rot}}$ and integrated Napierian absorbances $A$ associated with the molecules present in the cold part of supersonic expansion.

<table>
<thead>
<tr>
<th>Carrier gas / slm</th>
<th>H$_2$O</th>
<th>$T_{\text{rot}}$</th>
<th>$AR(0_{00})$</th>
<th>$AR(1_{01})$</th>
<th>$AP(1_{01})$</th>
<th>$AQ(1_{10})$</th>
<th>$AR(1_{10})$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>(para) $10^{-3}$</td>
<td>(ortho) $10^{-3}$</td>
<td>(ortho) $10^{-3}$</td>
<td>(ortho) $10^{-3}$</td>
<td>(ortho) $10^{-3}$</td>
</tr>
<tr>
<td>Ar, He, O$_2$ g/h</td>
<td>K</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>2</td>
<td>10.7 ± 1.8</td>
<td>0.754 ± 0.014</td>
<td>0.792 ± 0.012</td>
<td>1.36 ± 0.03</td>
<td>0.084 ± 0.004</td>
<td>0.067 ± 0.008</td>
</tr>
<tr>
<td>20</td>
<td>4</td>
<td>9.8 ± 1.5</td>
<td>1.56 ± 0.02</td>
<td>1.65 ± 0.02</td>
<td>2.78 ± 0.03</td>
<td>0.169 ± 0.006</td>
<td>0.178 ± 0.007</td>
</tr>
<tr>
<td>20</td>
<td>8</td>
<td>11.8 ± 1.2</td>
<td>2.21 ± 0.02</td>
<td>2.32 ± 0.02</td>
<td>3.86 ± 0.04</td>
<td>0.336 ± 0.007</td>
<td>0.316 ± 0.009</td>
</tr>
<tr>
<td>20</td>
<td>10</td>
<td>12.2 ± 0.4</td>
<td>2.58 ± 0.02</td>
<td>2.64 ± 0.02</td>
<td>4.36 ± 0.04</td>
<td>0.397 ± 0.007</td>
<td>0.374 ± 0.008</td>
</tr>
<tr>
<td>20</td>
<td>12</td>
<td>13.3 ± 0.2</td>
<td>2.74 ± 0.02</td>
<td>2.87 ± 0.03</td>
<td>4.72 ± 0.05</td>
<td>0.499 ± 0.010</td>
<td>0.478 ± 0.006</td>
</tr>
<tr>
<td>20</td>
<td>20</td>
<td>19.5 ± 0.7</td>
<td>3.31 ± 0.02</td>
<td>3.53 ± 0.03</td>
<td>5.82 ± 0.06</td>
<td>1.10 ± 0.01</td>
<td>1.010 ± 0.008</td>
</tr>
<tr>
<td>20</td>
<td>30</td>
<td>22.8 ± 1.0</td>
<td>3.36 ± 0.02</td>
<td>3.69 ± 0.03</td>
<td>6.31 ± 0.06</td>
<td>1.56 ± 0.01</td>
<td>1.45 ± 0.01</td>
</tr>
<tr>
<td>30</td>
<td>20</td>
<td>18.8 ± 0.1</td>
<td>2.33 ± 0.02</td>
<td>2.53 ± 0.03</td>
<td>4.37 ± 0.04</td>
<td>0.825 ± 0.018</td>
<td>0.749 ± 0.016</td>
</tr>
<tr>
<td>30</td>
<td>50</td>
<td>25.4 ± 0.2</td>
<td>2.69 ± 0.02</td>
<td>2.94 ± 0.02</td>
<td>5.07 ± 0.04</td>
<td>1.29 ± 0.01</td>
<td>1.20 ± 0.01</td>
</tr>
<tr>
<td>30</td>
<td>100</td>
<td>32.1 ± 0.4</td>
<td>2.77 ± 0.02</td>
<td>3.49 ± 0.03</td>
<td>6.09 ± 0.06</td>
<td>2.16 ± 0.02</td>
<td>2.01 ± 0.02</td>
</tr>
<tr>
<td>20</td>
<td>20</td>
<td>31.2 ± 0.6</td>
<td>1.25 ± 0.02</td>
<td>1.59 ± 0.02</td>
<td>2.75 ± 0.02</td>
<td>0.978 ± 0.016</td>
<td>0.884 ± 0.016</td>
</tr>
<tr>
<td>20</td>
<td>30</td>
<td>41.3 ± 1.2</td>
<td>0.28 ± 0.01</td>
<td>0.451 ± 0.006</td>
<td>0.786 ± 0.008</td>
<td>0.330 ± 0.007</td>
<td>0.328 ± 0.008</td>
</tr>
</tbody>
</table>

$^a$ average rotational temperature;

$^b$ $1_{01} \leftarrow 0_{00}$; $^c$ $2_{02} \leftarrow 1_{01}$; $^d$ $0_{00} \leftarrow 1_{01}$; $^e$ $1_{11} \leftarrow 1_{10}$; $^f$ $2_{11} \leftarrow 1_{10}$ transitions.
Figure 1: Selection of jet-cooled transmittance spectra recorded at 0.002 cm$^{-1}$ resolution to avoid line saturation effects. Water clustering, driven by the partial pressure of water vapor present in the flow, is one of the means used to control the temperature of the flow (argon in these examples). Rotational temperature increases from the lower to the upper panel as the water molar fraction increases. In our study, relative intensities were calculated using four ortho transitions (given using the notation “band $\nu_3$ ← ground state” by: $2_{02} ← 1_{01}$; $0_{00} ← 1_{01}$; $1_{11} ← 1_{10}$; $2_{11} ← 1_{10}$) and one para transition ($1_{01} ← 0_{00}$).
Figure 2: Series of low resolution absorbances (offset for clarity) of water vapor cooled in argon (400 co-added scans at 1 cm\(^{-1}\) resolution). Water clustering is driven by the water vapor partial pressure (as indicated in the rightmost part of the figure) in the stagnation reservoir. In addition to the partially resolved water monomer lines, both the signatures of free OH (around 3710 cm\(^{-1}\)) and bound OH vibrations are observed. The signatures of the water dimer and trimer can be seen at 3601 and 3533 cm\(^{-1}\), respectively, for conditions leading to weak clustering. The broad absorption observed below 3600 cm\(^{-1}\), corresponds to much larger water clusters that form at enhanced water vapor partial pressure.
Figure 3: Impact pressure measured by a Pitot probe (a). This 2D map was used to visualize the flow structure in a section perpendicular to the long edge of the slit, resulting from an expansion of argon under conditions very similar to those used for the spectral recordings ($P_0 = 1072$ hPa, $P_{ch} = 0.683$ hPa, $T_0 = 295$ K, slit width: 18 microns, slit length: 60 mm). The path of the infrared beam is indicated by the dashed lines (circle = focal point; ellipse = edges of the slit). Various flow parameters have been extracted from measurements relative to the plane of symmetry: Knudsen number (b); Mach number (c); translational temperature (d) compared to a calculation using the method of characteristics (solid line); molecular density (e) compared to a calculation using the method of characteristics (solid line).
Figure 4: Concentration of condensed water vapor in an expansion of argon. These values, estimated from the measured monomer absorption, reveal a strong water condensation (between 65 and 83 %) even for small partial pressures of water vapor.
Figure 5: Example of rotational diagram used to extract the rotational temperature from absorbance spectra in the case of the presence of hot and cold molecules in the path of the infrared beam (here 100 g/h of H₂O in 30 slm of Argon). The quantity \( \frac{N L n_i}{(2J + 1)} \) (see Eq. 10) extracted from the fitting of the different lines, is represented as a function of the energy level \( E_i \) of the initial state of the transition. The open circles and open squares represent the data obtained with a single Gaussian profile for ortho and para lines respectively. The data for energies \( E_i \) higher than 190 K follow a straight line and the slope gives the rotational temperature of the hot molecules \((251 \pm 11 \text{ K})\). The warm gas contribution is then removed from the low-\( J \) rotational line absorption by a fitting procedure taking into account the hot and cold contributions (see text for details), leading to a corrected value of the cold gas rotational temperature for the ortho molecules \((32.3 \pm 0.4 \text{ K})\) very close to the rotational temperature extracted from the lines associated with the para molecules \((31.9 \pm 0.4 \text{ K})\). A total of 8 low-\( J \) rotational lines have been used to estimate the cold rotational temperature.
Figure 6: Absorptance of the $1_{11} \leftarrow 1_{10}$ transition observed with a flow of 100 g/h of water in 30 slm of Ar. The experimental data (line) are compared to the calculated data (dashed line) after a fitting procedure (a) with a single Gaussian profile and (b) with two Gaussian profiles associated with one contribution coming from “hot” gas (red dash lines) and one contribution from “cold” gas (blue short dash-dot line) convoluted by the appropriate apodization function (Boxcar). The obs-calc residue is depicted in the bottom part of each panel.
Figure 7: Relative integrated absorbances $A_{101 \rightarrow 0_{00}} / A_{2_{02} \rightarrow 1_{01}}$ measured as a function of rotational temperature. The expected behaviour in case of Slow NSC (solid line) and in case of Fast NSC (dashed line) is also represented. The uncertainty of 10% on the theoretical values are shown in gray are derived from HITRAN$^{32}$ data. Triangle symbols represent data obtained in pure oxygen or in a mixture with equal Ar and O$_2$ flow rates as a carrier gas, as shown in Table 3, whereas the star refers to the data obtained in an expansion of He instead of Ar as a carrier gas. The x-axis error bars reflect the uncertainty of the rotational temperature retrieved from the rotational diagram. The y-axis error bars originate from the most severe estimate of uncertainty in the line intensities measurements following subtraction, when possible, of the hot gas contribution to the low-temperature line absorption.
Figure 8: Relative integrated absorbances $A_{1_{01} \leftarrow 0_{00}} / A_{0_{00} \leftarrow 1_{01}}$ measured as a function of rotational temperature. See Fig. 7 caption for more details.
Figure 9: Relative integrated absorbances $A_{10\leftarrow 0_0}/A_{1_{11}\leftarrow 1_{10}}$ measured as a function of rotational temperature. See Fig. 7 caption for more details.
Figure 10: Relative integrated absorbances $A_{101-0_00}/A_{211-1_{10}}$ measured as a function of rotational temperature. See Fig. 7 caption for more details.
Graphical Abstract
$T_{rot} = 32.1 \pm 0.4 \text{K}$

$T_{rot} = 13.3 \pm 0.2 \text{K}$

$T_{rot} = 9.8 \pm 1.5 \text{K}$

$\chi = 6.47\%$

$\chi = 1.23\%$

$\chi = 0.41\%$
Shock cells

Distance from nozzle exit (cm)

Distance from nozzle / cm

Translational temperature / K

Molecular density / $10^{18}$ cm$^{-3}$
Partial pressure of water vapor in the reservoir (hPa)
\[ T_{\text{para}} = 31.9 \pm 0.4 \text{ K} \]

\[ T_{\text{ortho}} = 32.3 \pm 0.4 \text{ K} \]

\[ T_{\text{hot}} = 251 \pm 11 \text{ K} \]
(a) Absorbance vs. Wavenumbers (cm$^{-1}$)

(b) Absorbance vs. Wavenumbers (cm$^{-1}$) with contributions from cold and hot molecules.
\[ \frac{AR(0_{00})}{AR(1_{01})} \]
AR(0_00) / AQ(1_10)
\[ \frac{AR(0_{00})}{AR(1_{10})} \]